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De La Salle University, Manila, Philippine (Hybrid Conference)

## Swarm Intelligence for Shape Reconstruction in the Context of the European Project PDE-GIR: Recent Advances and Future Trends



PDE-GIR

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Bournemouth  
University



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UTM  
UNIVERSITI  
TEKNOLOGI  
MALAYSIA



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## Outline of this talk

1. PDE-GIR Project
2. Shape Reconstruction Problem
3. PDE+Artificial Intelligence for SR
4. Some Illustrative Examples
5. Future Research



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## PDE-GIR project



PDE-GIR

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PDE-GIR project is aimed at developing advanced PDE based techniques, exploiting their applications through exchanges of research and innovation staff, international and intersectoral collaborations, and knowledge transfer.



EU H2020 MSCA-RISE Program

Jan. 2018 - Oct. 2023

535,000€ (direct funding)

PDE-BASED GEOMETRIC MODELLING, IMAGE  
PROCESSING AND SHAPE RECONSTRUCTION



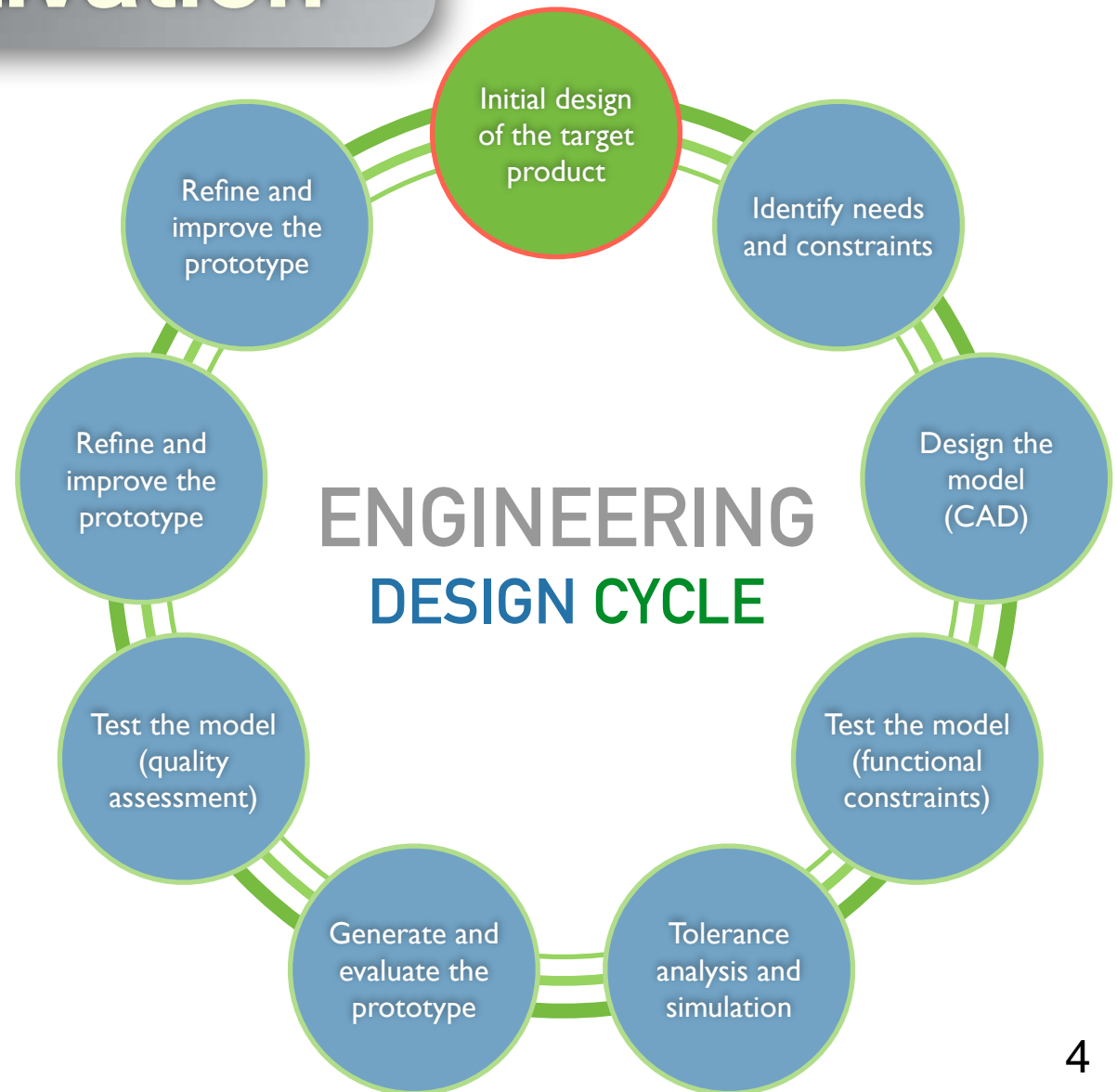
PDE-GIR



## Motivation

### FORWARD ENGINEERING

1. Design (**CAD model**)
2. Test & Analysis
3. Prototype generation
4. Refine & Improve
5. Industrial manufacturing
6. Final **physical product**





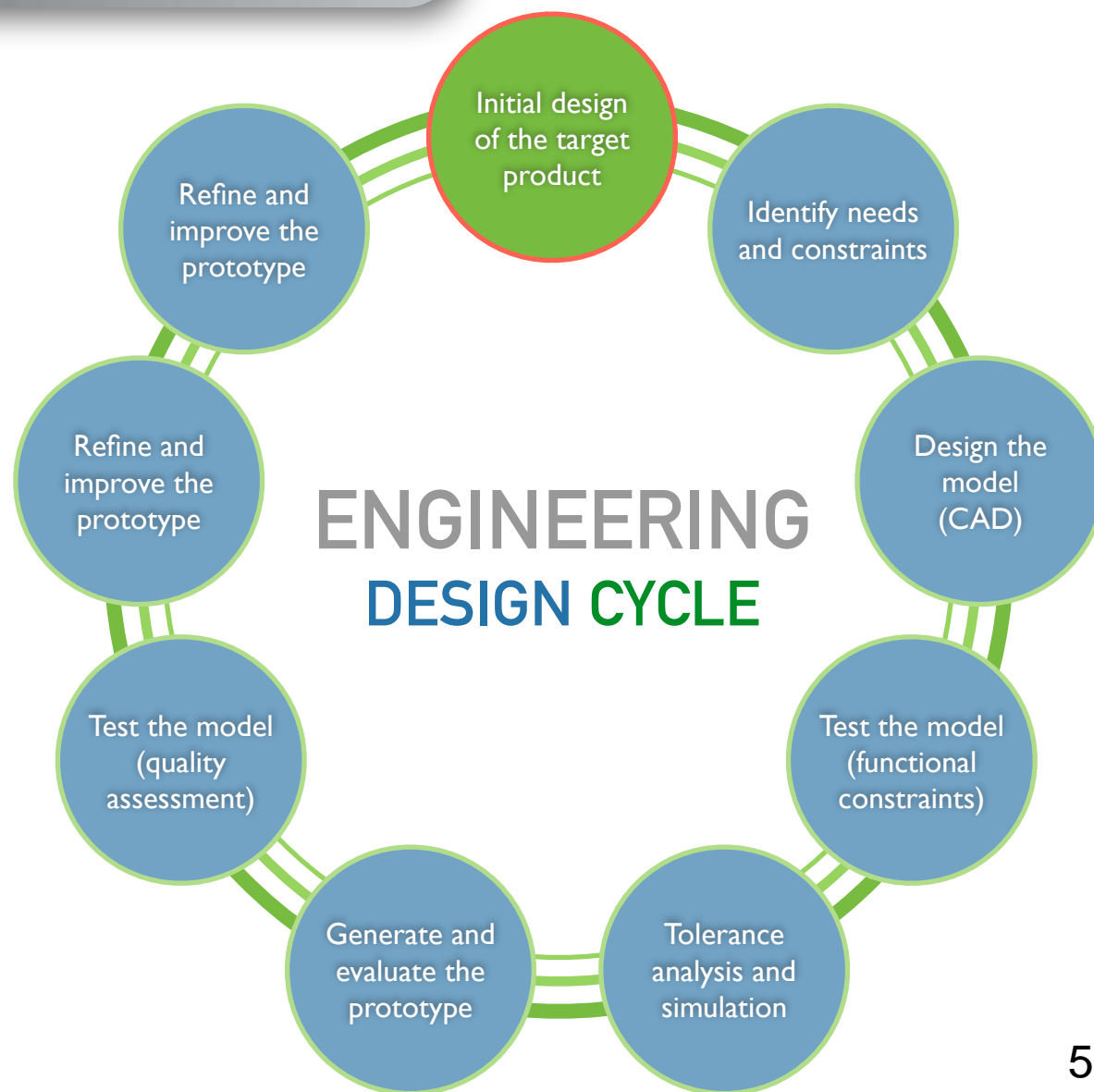
## Motivation

### FORWARD ENGINEERING

1. Design (**CAD model**)
2. Test & Analysis
3. Prototype generation
4. Refine & Improve
5. Industrial manufacturing
6. Final **physical product**

### REVERSE ENGINEERING

1. **Physical product**
2. 3D scanning
3. Point cloud data
4. Surface reconstruction
5. Test & Analysis
6. Final **CAD model**



## Motivation



Product Manufacturing

Model accuracy

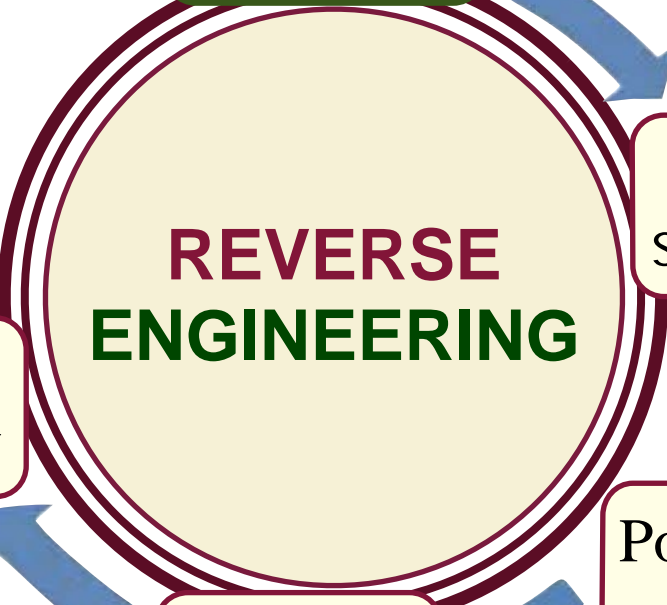
Physical model



3D scanning



Point cloud data



Surface model





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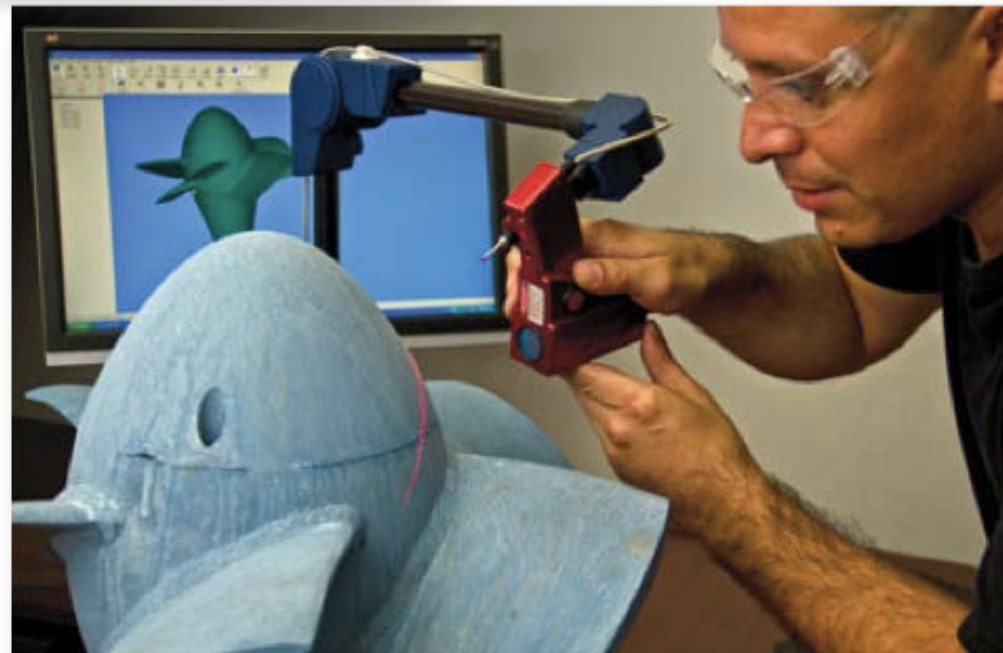
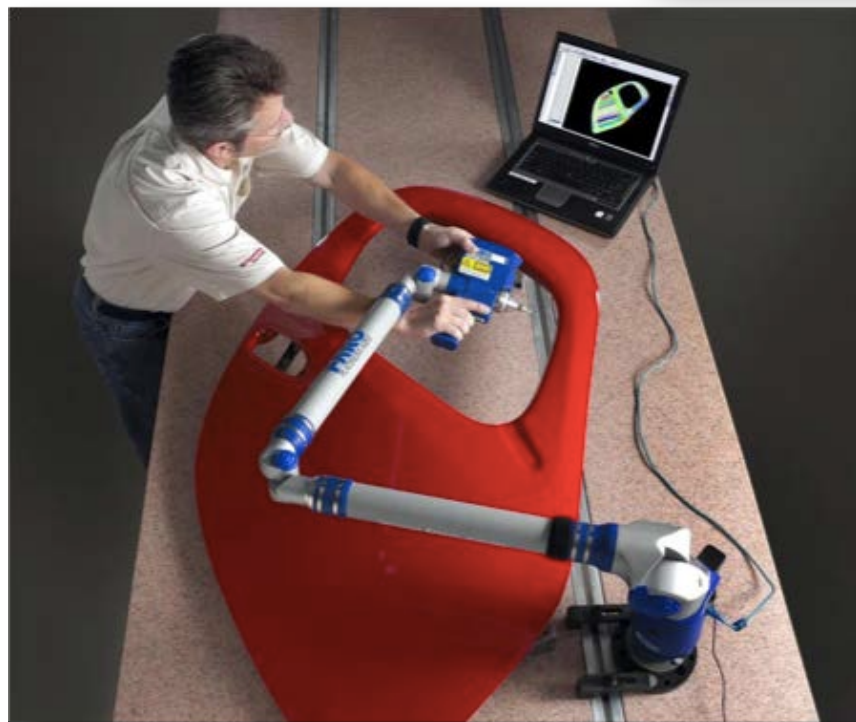
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## Motivation





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## Motivation





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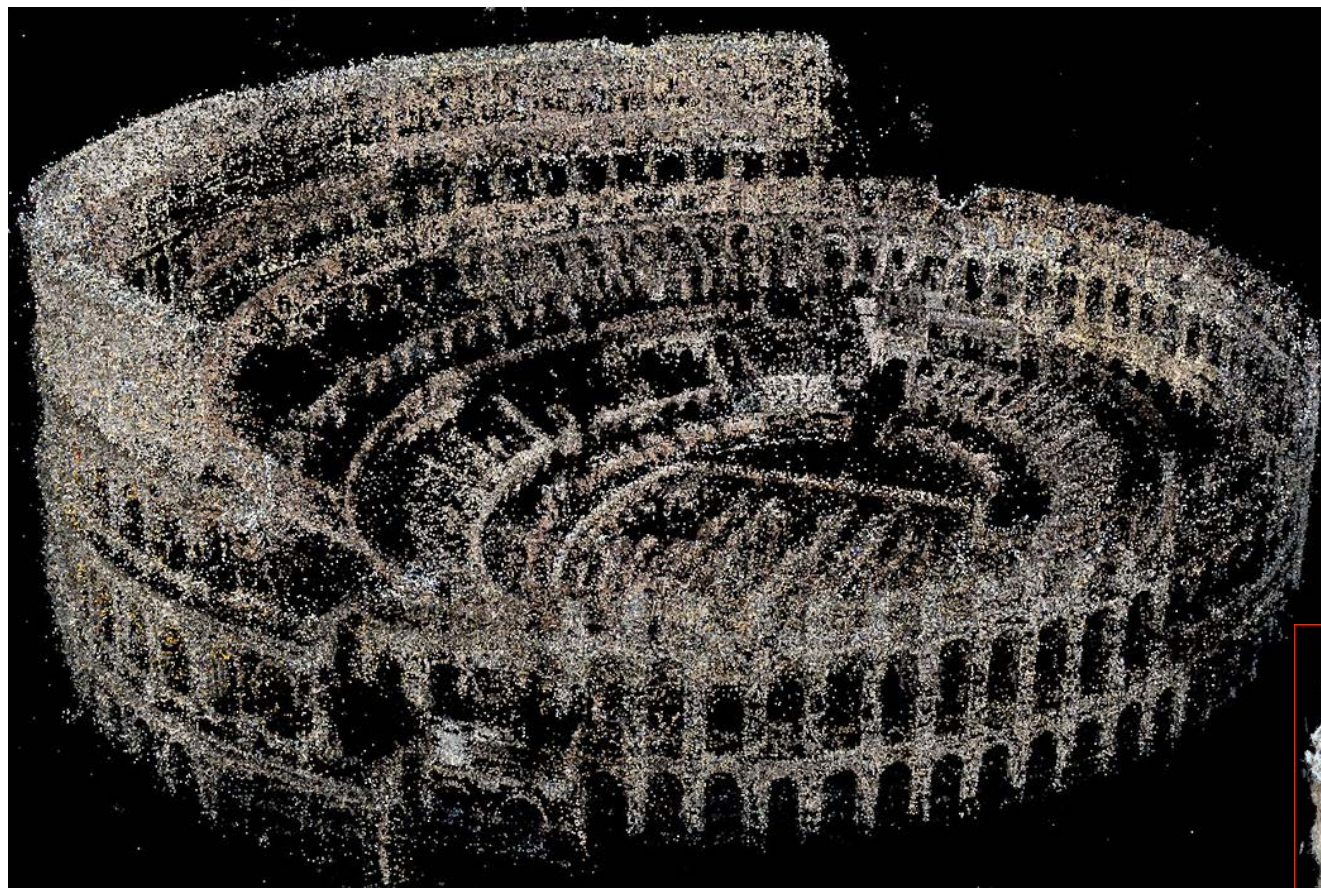
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Point cloud

Mesh Model



**ROMAN COLISEUM**  
(Univ. Washington)



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## Motivation

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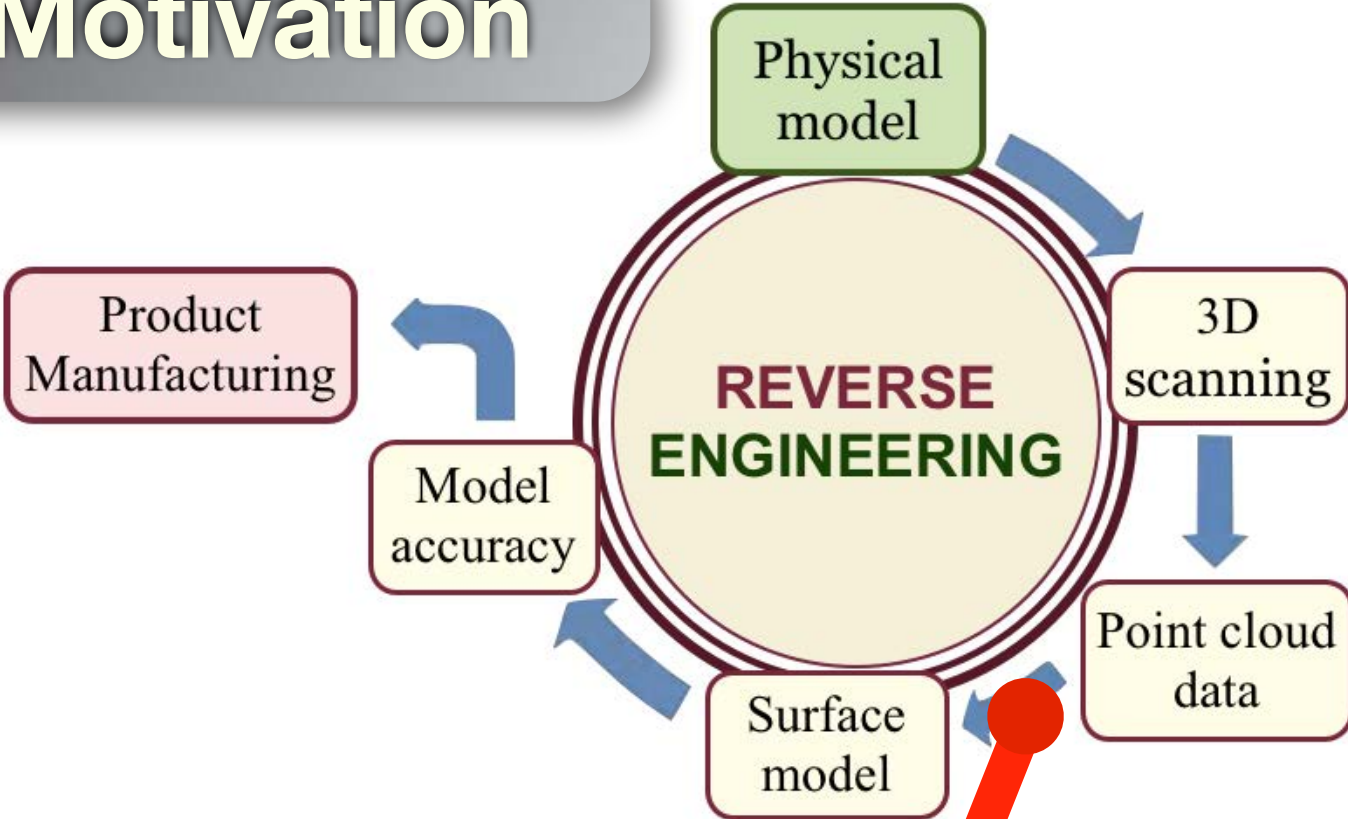
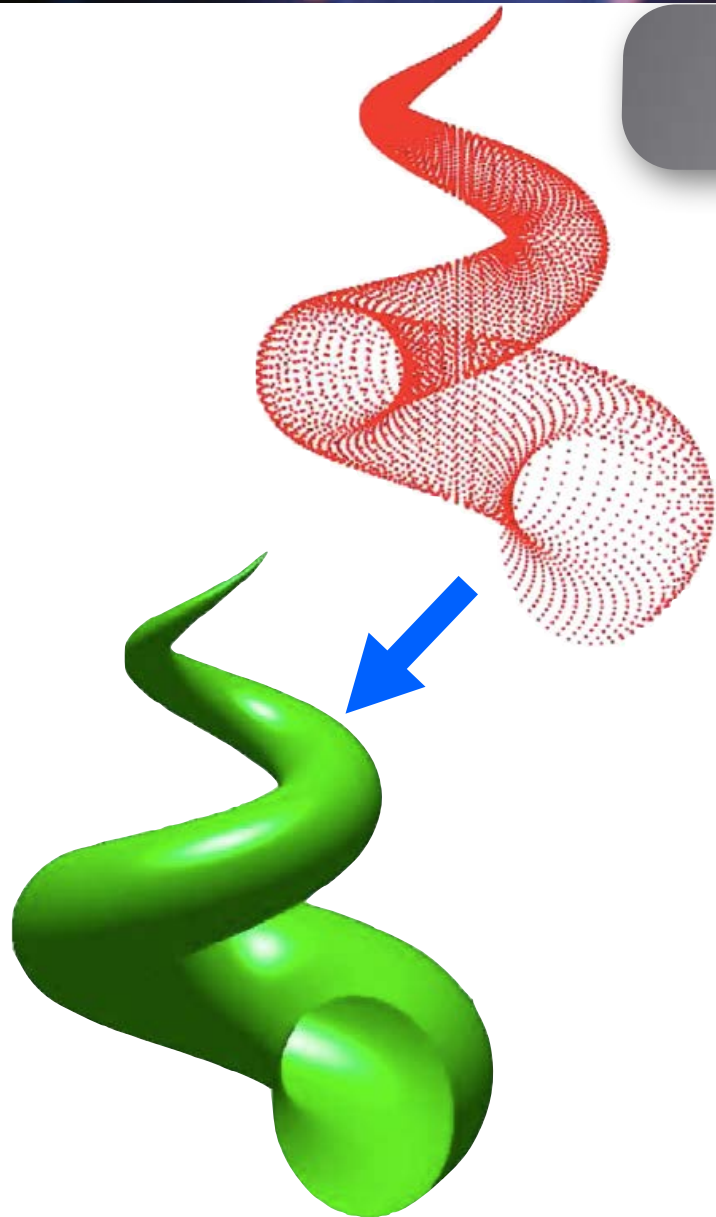
## Motivation

### REVERSE ENGINEERING IN INDUSTRY

#### What for?

1. Gain knowledge about how a product works
2. Repurpose obsolete products
3. Analyze the quality of shape
4. Intellectual/Industrial property infringement assessment
5. Modify the original product shape for mass customization

## Motivation



**SURFACE RECONSTRUCTION**



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By **surface reconstruction** we mean the construction of an **unknown surface** (implicit, parametric, free-form, etc.) from a **given input** (cross sections, profile curves, data points, etc.)

**Input:**

- **cross-sections**
- **clouds of data points**
- **profile curves**
- **mixed information**

**Output:**

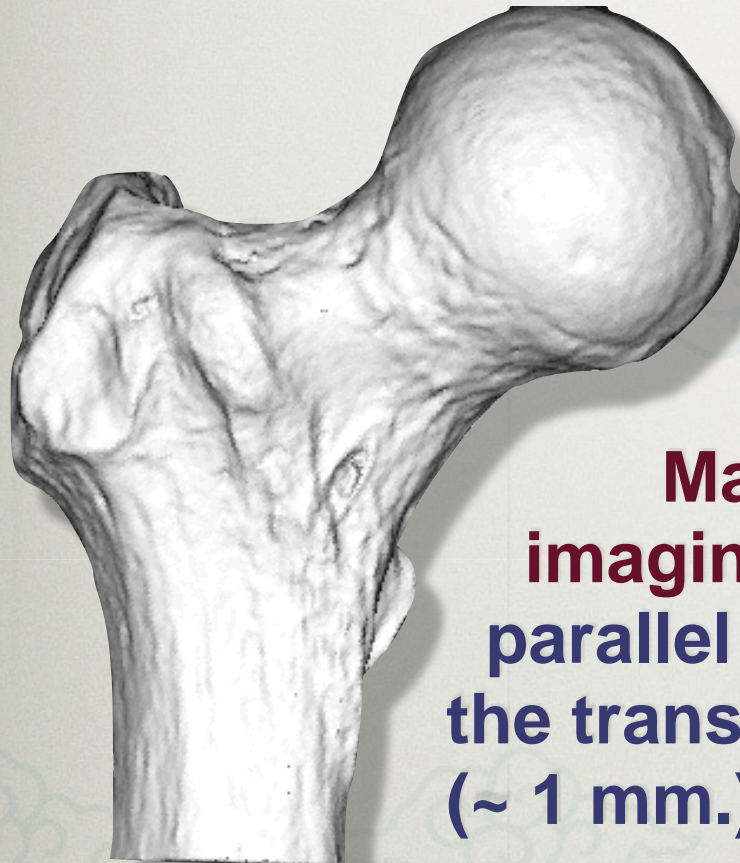
- **implicit surfaces**
- **polynomial surfaces**
- **rational surfaces**
- **free-form surfaces**



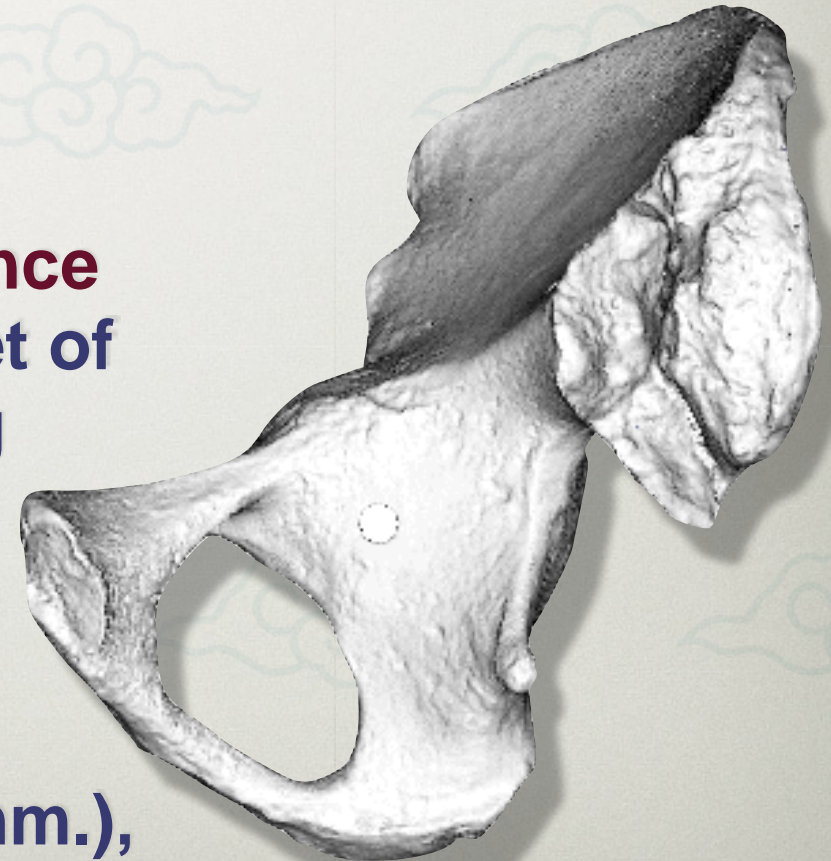
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**Computer tomography:** scanned projections from different point-views to generate a 3D volume



**Magnetic resonance imaging:** input is a set of parallel sections along the transversal axis (~ 1 mm.)



**Others:** confocal microscopy (~ $10^{-4}$  mm.), electron microscopy (~ $10^{-8}$  mm.), etc.



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## However, many classical optimization techniques tend to fail when:

- The objective function is **not differentiable**
- The objective function is computed through a **black-box** procedure
- Little or **no information** about the problem is given
- Derivatives are **too difficult or expensive** to obtain
- It is expected that **many optima exist**
- Data are affected by **noise, missing data or other artifacts**



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## When using metaheuristic methods?

- An easy problem with **very large instances**
- An easy problem with **hard real-time constraints**
- **Difficult problems** with medium size and/or difficult input structures
- Optimization problems with **time-consuming objective functions and/or constraints**
- Non-analytical models of optimization problems: **black box scenario** (objective function)
- **Non-deterministic complex models**: uncertainty, robust optimization, dynamic, multi-objective,...
- **Non-differentiable** (even non-continuous) underlying functions of data
- Input data subjected to **noise, imperfect sampling and other artifacts**



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## Metaheuristic methods:

### Advantages:

- Generally produce **higher quality results** (given enough time) than simple heuristics
- Make **few (or none) assumptions** about your problem
- Are very **general** (can be used when nothing else works)

### Drawbacks:

- They **take a lot longer** as they have to generate and evaluate many solutions rather than just one heuristics
- **Parameter tuning** is always a challenge
- **Convergence to optima is not guaranteed**

NO FREE LUNCH THEOREM



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## Some **metaheuristic** methods:

TYPE	METHOD	COMMENTS
EARLY WORKS	Tabu Search	Glover (1986)
	Random Search	Rastrigin (1963)
	Pattern Search	Hooke & Jeeves (1961)
	Grammatical Evolution	Ryan et al (1998)
	Path Relinking	Glover (1996)
PHYSICS & CHEMISTRY INSPIRED	Simulated Annealing	Kirkpatrick et al. (1983)
	Stochastic Diffusion Search	Bishop (1989)
	Harmony Search	Geem et al. (2001)
	Intelligent Water Drops	Shah-Hosseini (2007)
	Electromagnetism Approach	Birbil & Fang (2003)



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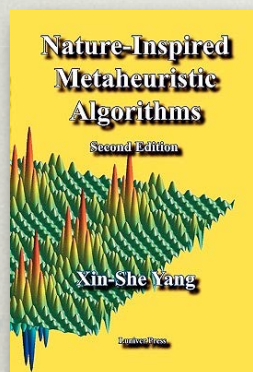
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Some other popular metaheuristic methods:



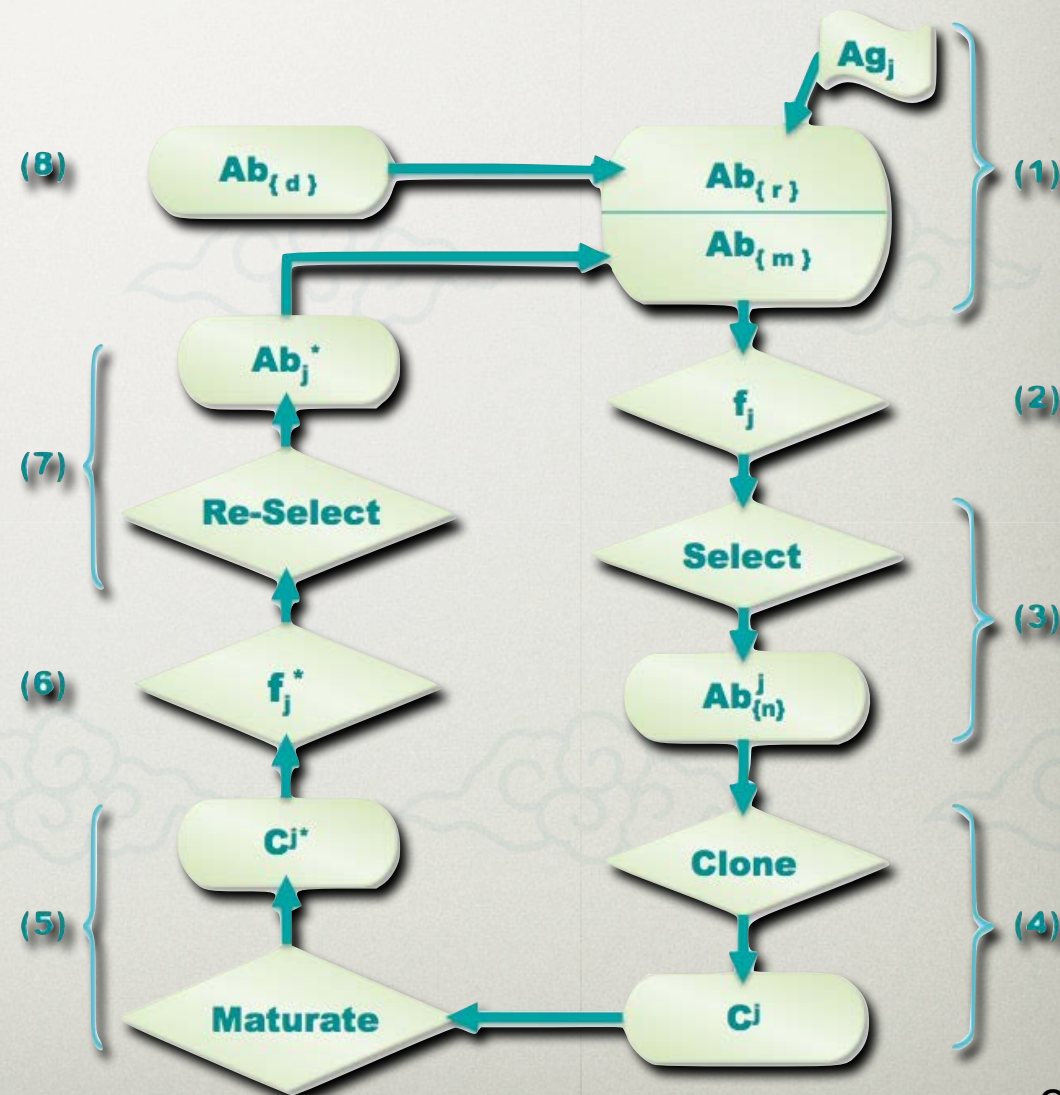
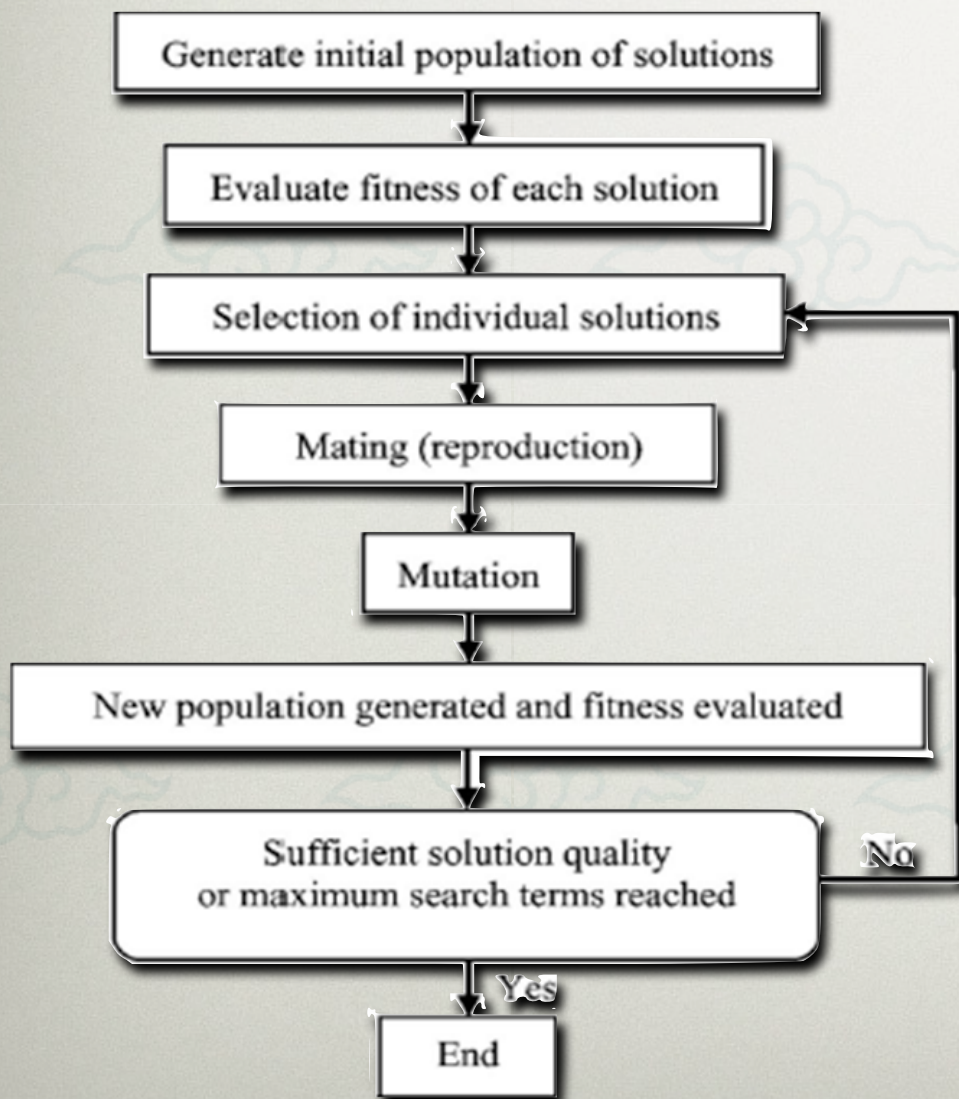
Xin-She Yang: *Nature-Inspired Metaheuristic Algorithms (2nd. Edition)*. Luniver Press (2010)

TYPE	METHOD	COMMENTS
SWARM INTELLIGENCE	Ant Colony Optimization	Marc Dorigo (1992)
	Particle Swarm Optimization	Kennedy & Eberhart (1995)
	Artificial Immune Systems	
	Firefly Algorithm	Xin-She Yang (2009)
	Artificial Bee Colony	Karaboga & Basturk (2007)
	Bee Colony Optimization	Lučić & Teodorović (2001)
	Cuckoo Search	Xin-She Yang (2011)
BIO-INSPIRED	Genetic Algorithms	Holland (1975)
	Differential Evolution	Storn & Price (1997)
	Bio-geography optimization	Dan Simon (2008)
	Evolutionary Computing	
	Genetic Programming	Koza (1992)
	Bacterial Foraging	Passino (2002)
	Random Search	Rastrigin (1963)
	Pattern Search	Hooke & Jeeves (1961)
	Grammatical Evolution	Ryan et al (1998)



## Genetic Algorithms (GA)

## Artificial Immune Systems (AIS)





## Particle Swarm Optimization

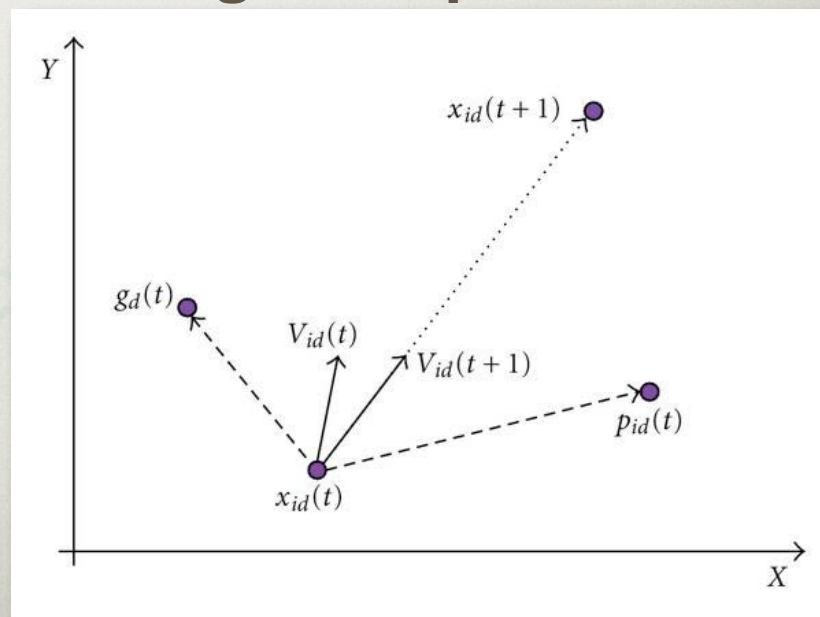
$$R_1, R_2 \in U[0, 1]$$

$$V_i^{k+1} = w V_i^k + \gamma_1 R_1 [P_{g,b}^k - P_i^k] + \gamma_2 R_2 [P_{i,b}^k - P_i^k]$$

iteration (blue arrow pointing to  $V_i^{k+1}$ )  
 inertia weight (red arrow pointing to  $w$ )  
 global best position (dark red arrow pointing to  $P_{g,b}^k$ )  
 particle's best position (green arrow pointing to  $P_{i,b}^k$ )  
 velocity of particle i (red arrow pointing to  $V_i^k$ )  
 social parameter (blue arrow pointing to  $\gamma_1$ )  
 cognitive parameter (brown arrow pointing to  $\gamma_2$ )

$$P_i^{k+1} = P_i^k + V_i^k$$

iteration (blue arrow pointing to  $P_i^{k+1}$ )  
 position of particle i (green arrow pointing to  $P_i^k$ )





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## The Firefly Algorithm

### The Algorithm

#### Begin

- 1) Objective function:  $f(x)$
- 2) Generate an initial population of  $n$  fireflies  $x(i)$
- 3) Formulate light intensity  $I$  associated with  $f(x)$
- 4) Define absorption coefficient  $\gamma$

#### While (t < MaxGeneration)

```
for i=1:n
  for j=1:n
    if  $I(i) > I(j)$ , then move firefly  $i$  towards  $j$ 
    end if
    Vary attractiveness with distance  $r$  via  $\exp(-\gamma r)$ ;
    Evaluate new solutions and update light intensity;
  end for j
end for i
Rank fireflies and find the current best;
```

#### end while

Post-processing the results and visualization;

#### end





A. Gálvez, A. Iglesias, : “Particle swarm optimization for non-uniform rational B-spline surface reconstruction from clouds of 3D data points”. **Information Sciences** (I.F. 8.1). Vol. 192 (1), 174-192 (2012)



## Basic Data:

- NURBS 20412 parameters
- 9150 data points



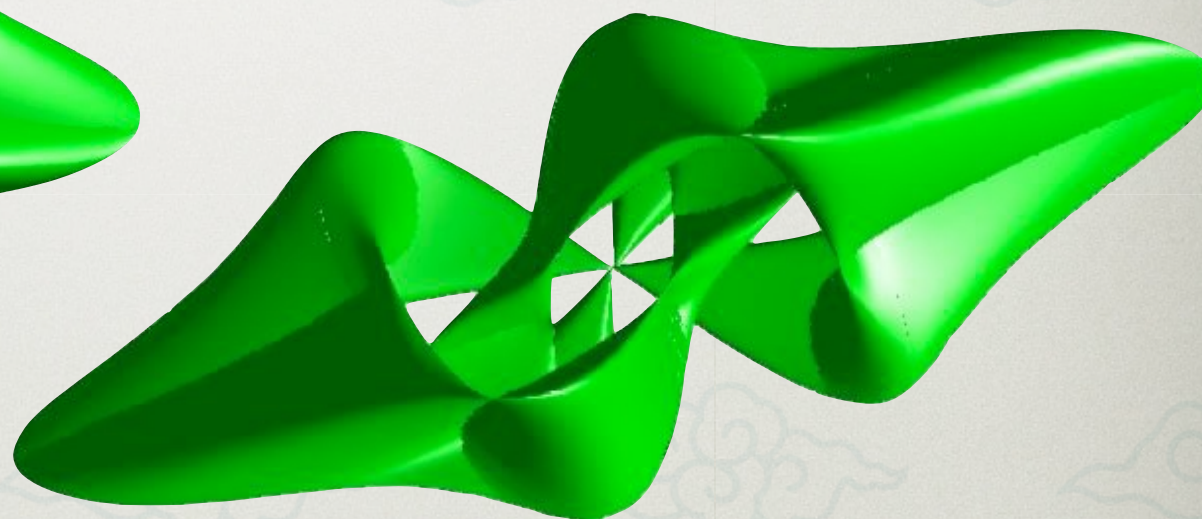
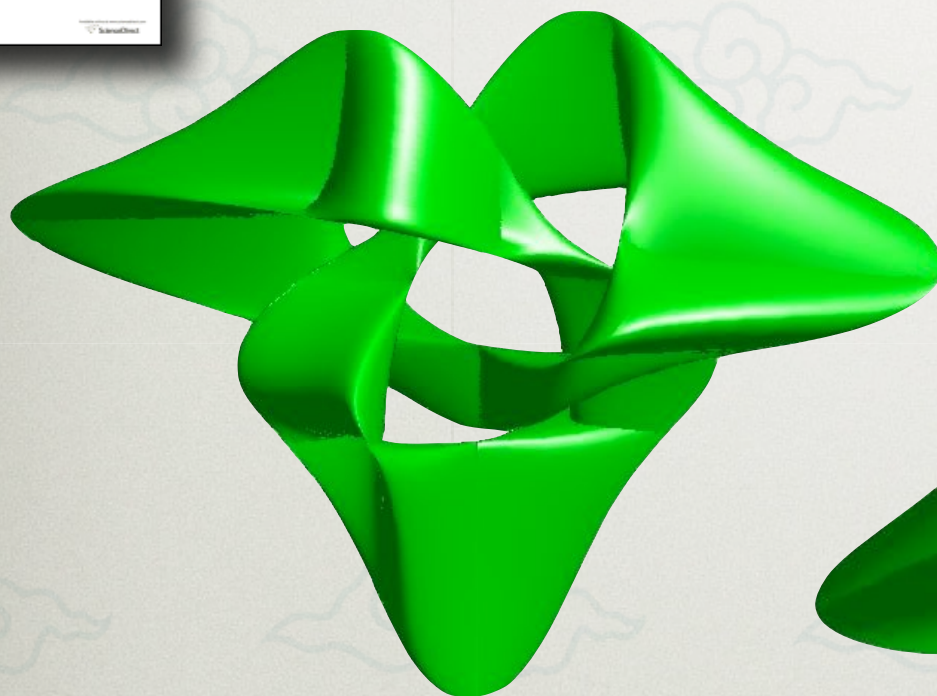
## Results:

- CPU time: <4 min.
- error:  $10^{-12}$  -  $10^{-14}$





A. Gálvez, A. Iglesias,: “Particle swarm optimization for non-uniform rational B-spline surface reconstruction from clouds of 3D data points”. **Information Sciences** (I.F. 8.1). Vol. 192 (1), 174-192 (2012)



## Basic Data:

- NURBS 9557 parameters
- 4132 data points

## Results:

- CPU time: <3 min.
- error:  $10^{-13}$  -  $10^{-14}$



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A. Gálvez, A. Iglesias, J. Puig-Pey: *“Iterative two-step genetic-algorithm-based method for efficient polynomial B-spline surface reconstruction”*.

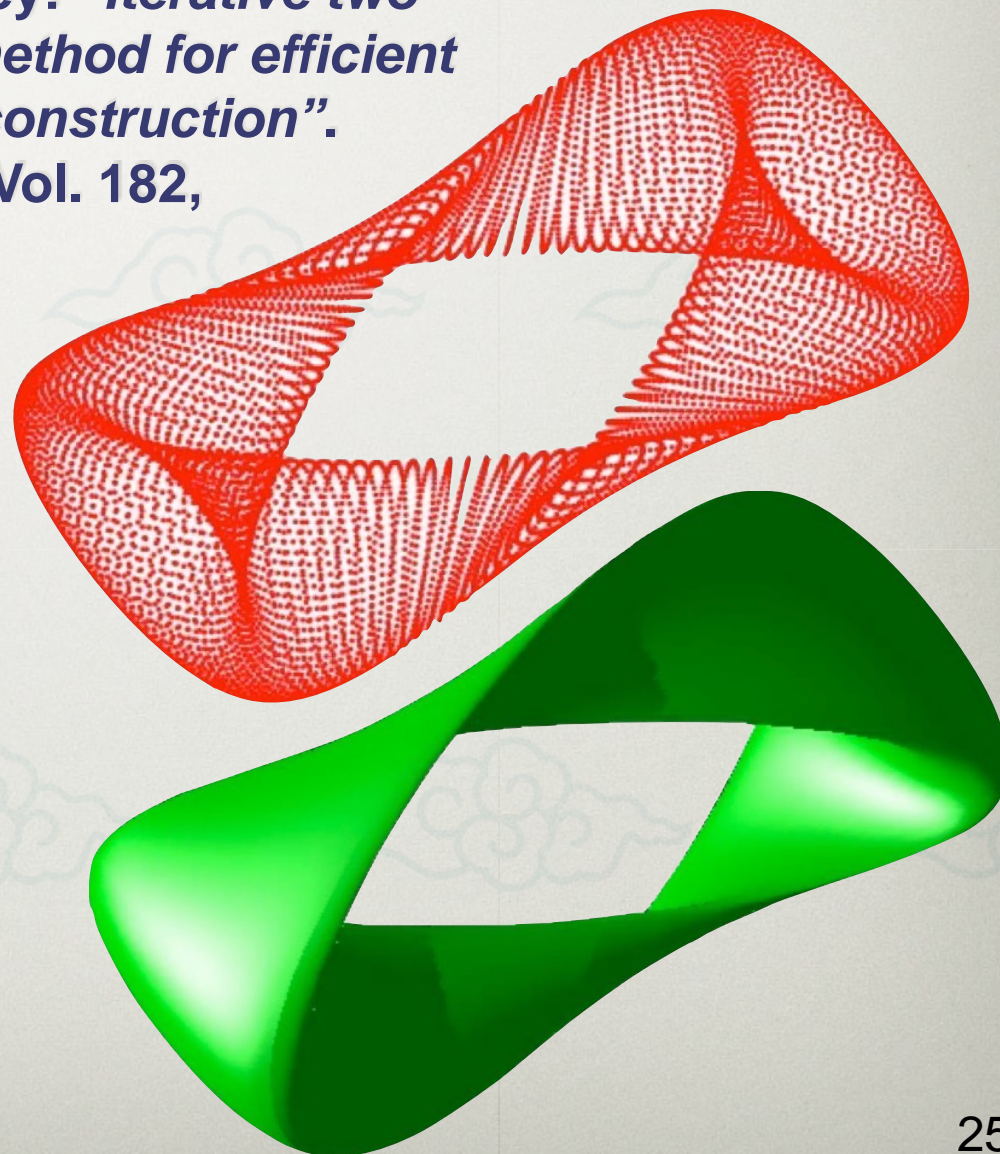
**Information Sciences** (I.F. 8.1), Vol. 182,  
Issue 1, 56-76 (2012)

## Basic data:

- **NURBS surface**
- **20933 parameters**
- **10500 data points**

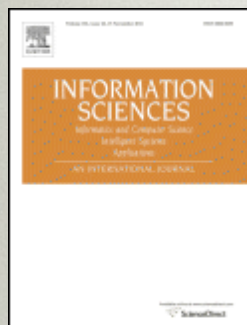
## Results:

- **CPU time: 2-3 h.**
- **error:  $10^{-15}$**





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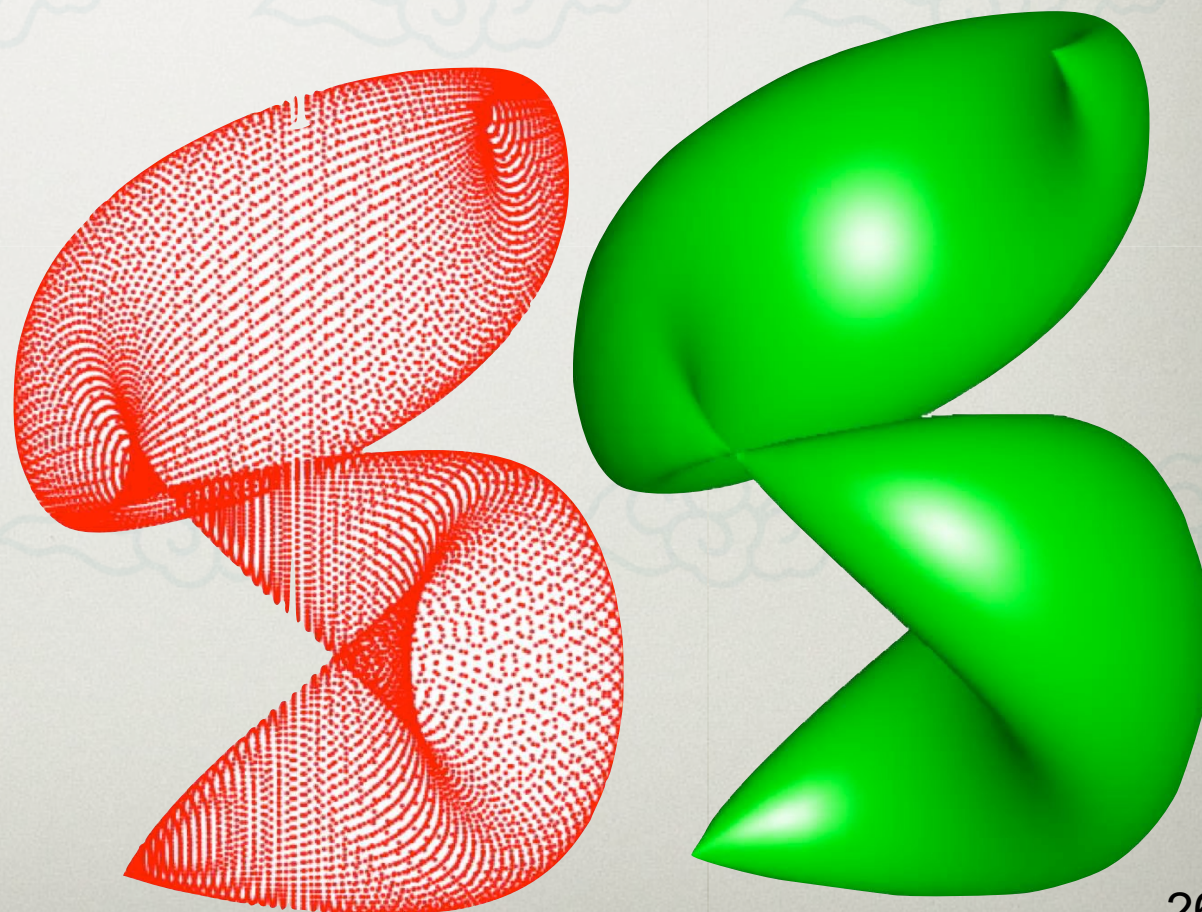
A. Gálvez, A. Iglesias, J. Puig-Pey: *“Iterative two-step genetic-algorithm-based method for efficient polynomial B-spline surface reconstruction”*. **Information Sciences (I.F. 8.1)**, Vol. 182, Issue 1, 56-76 (2012)

## Basic data:

- **NURBS surface**
- **29280 parameters**
- **14200 data points**

## Results:

- **CPU time: 14-20 min.**
- **error:  $10^{-11}$**

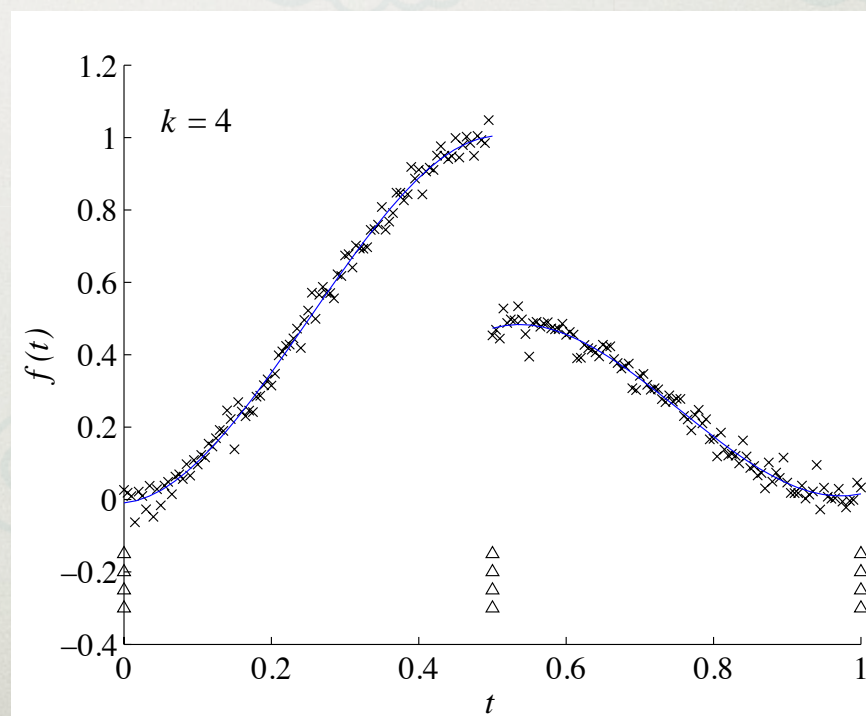
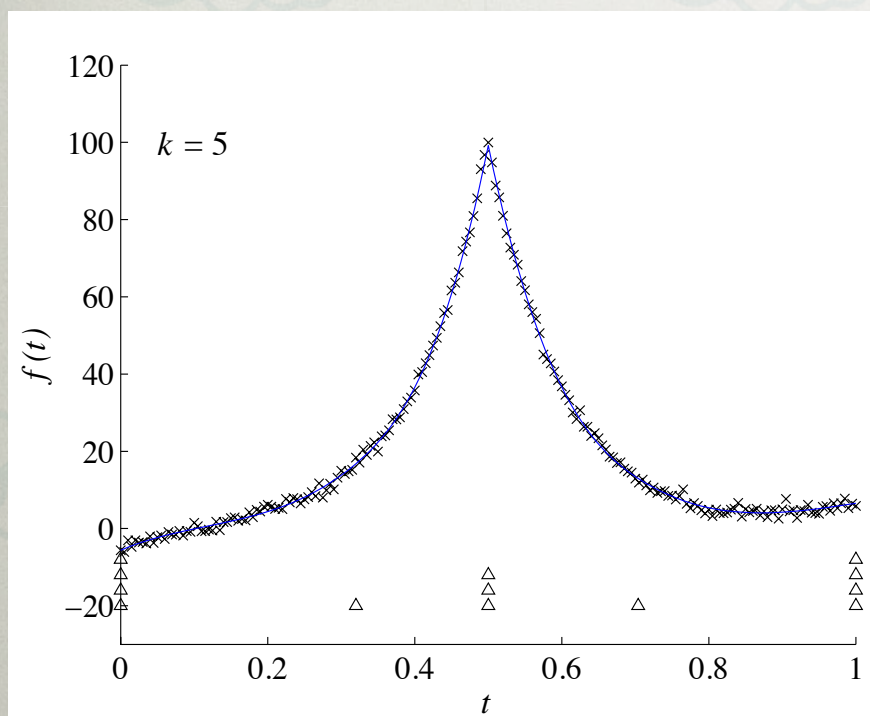




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A. Gálvez, A. Iglesias: *“Efficient PSO Approach for Data Fitting with Free Knot B-splines”*. **Computer Aided Design (I.F. 4.3)**, Vol. 43, Issue 12, 1683-1692 (2011)

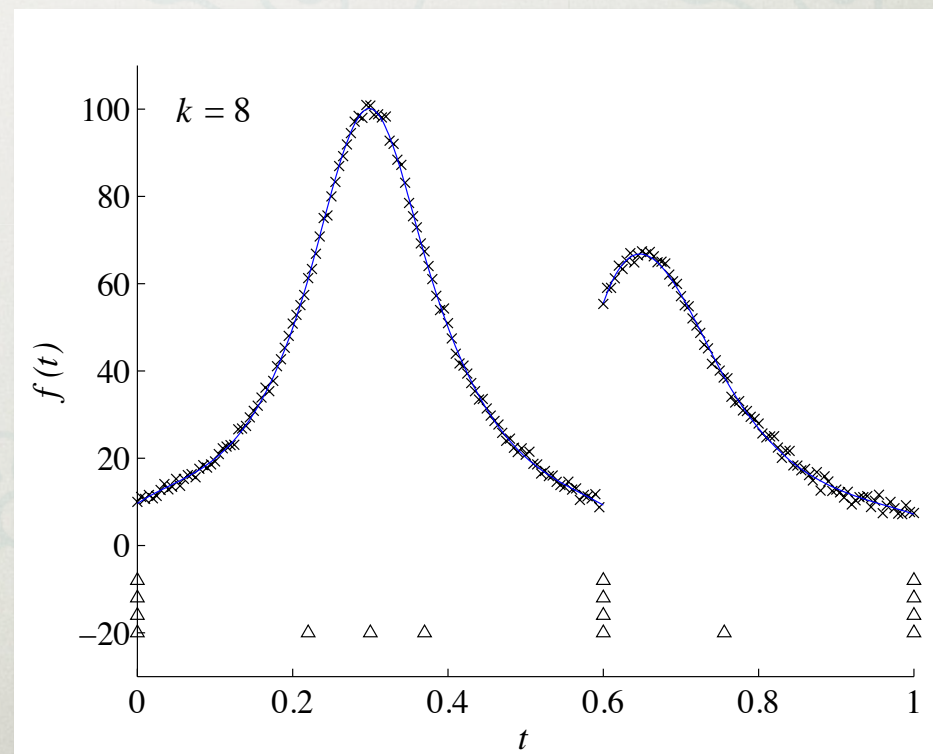
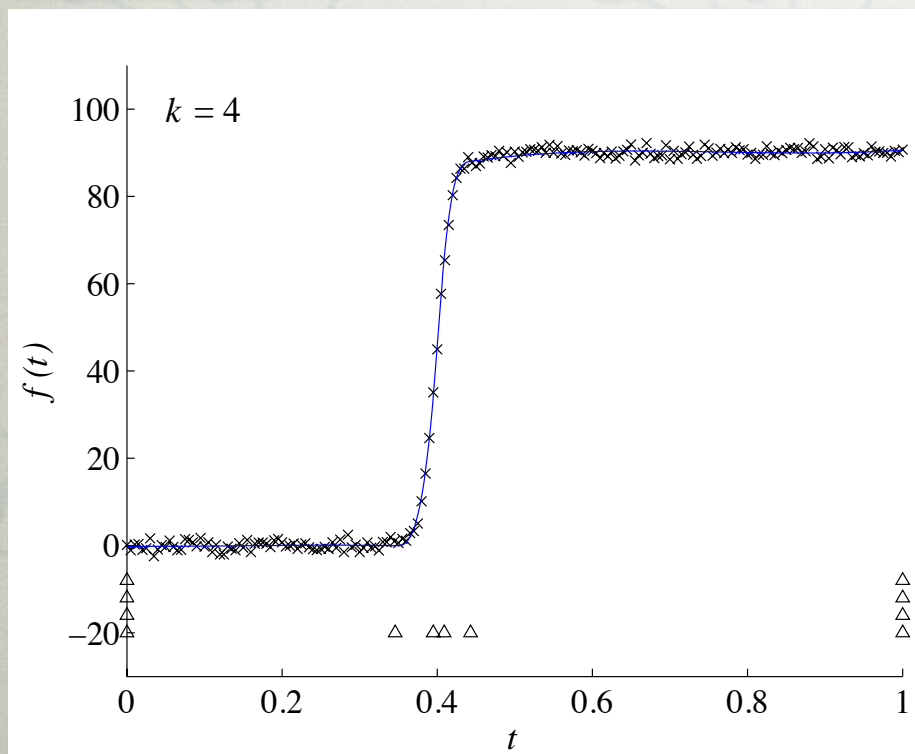




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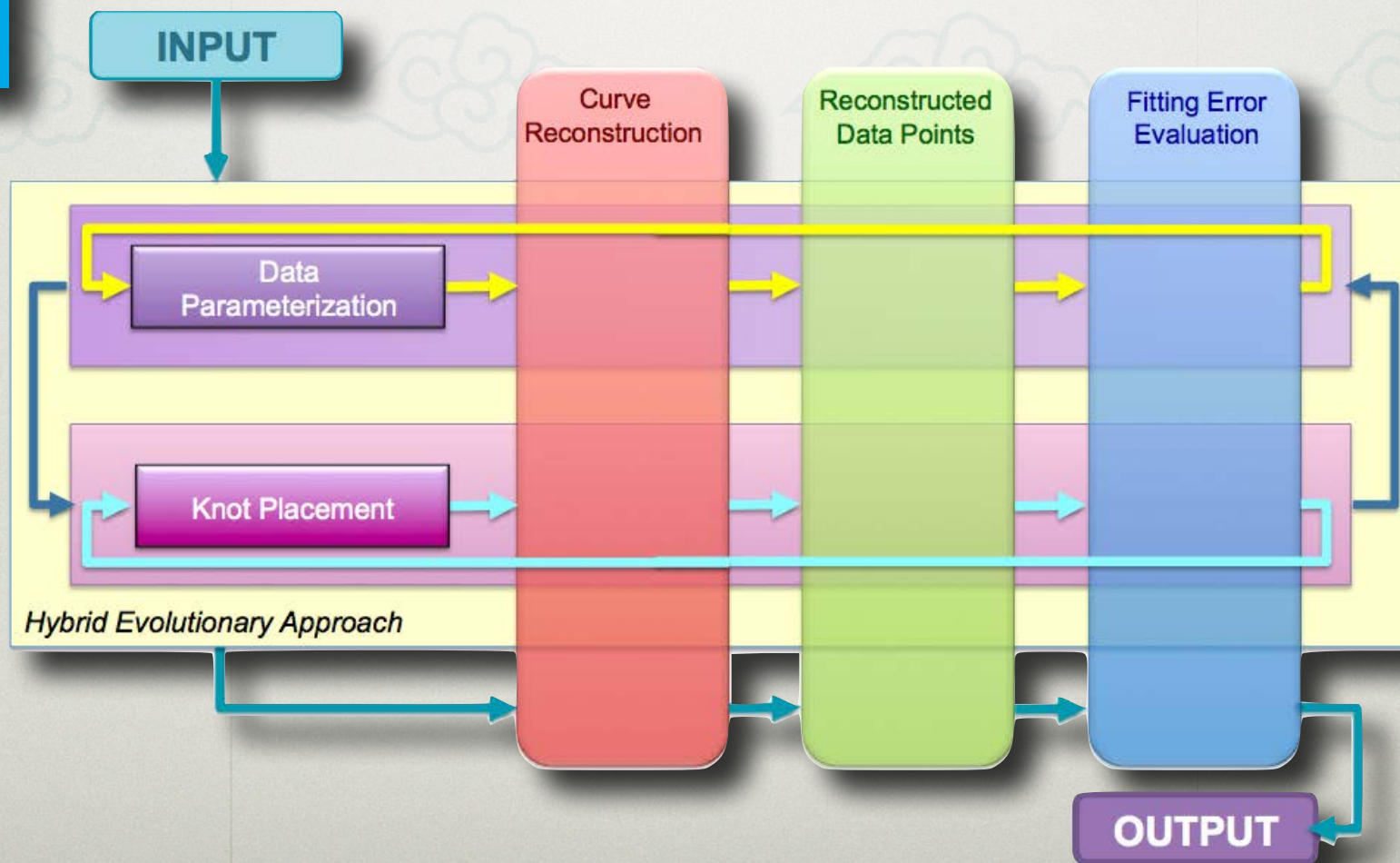




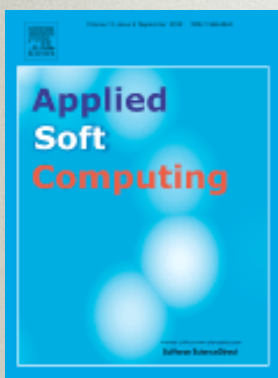
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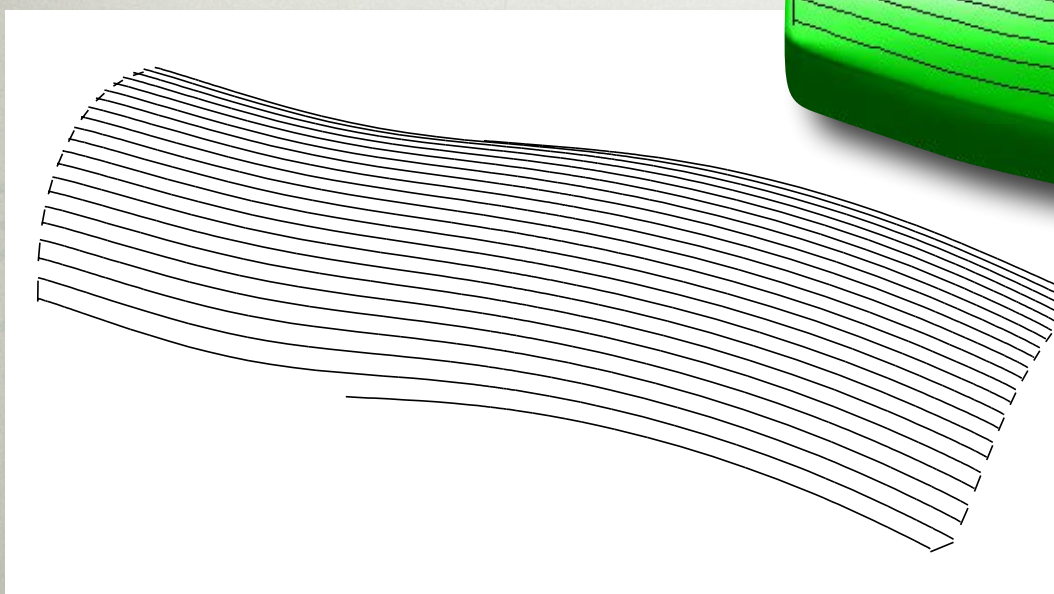
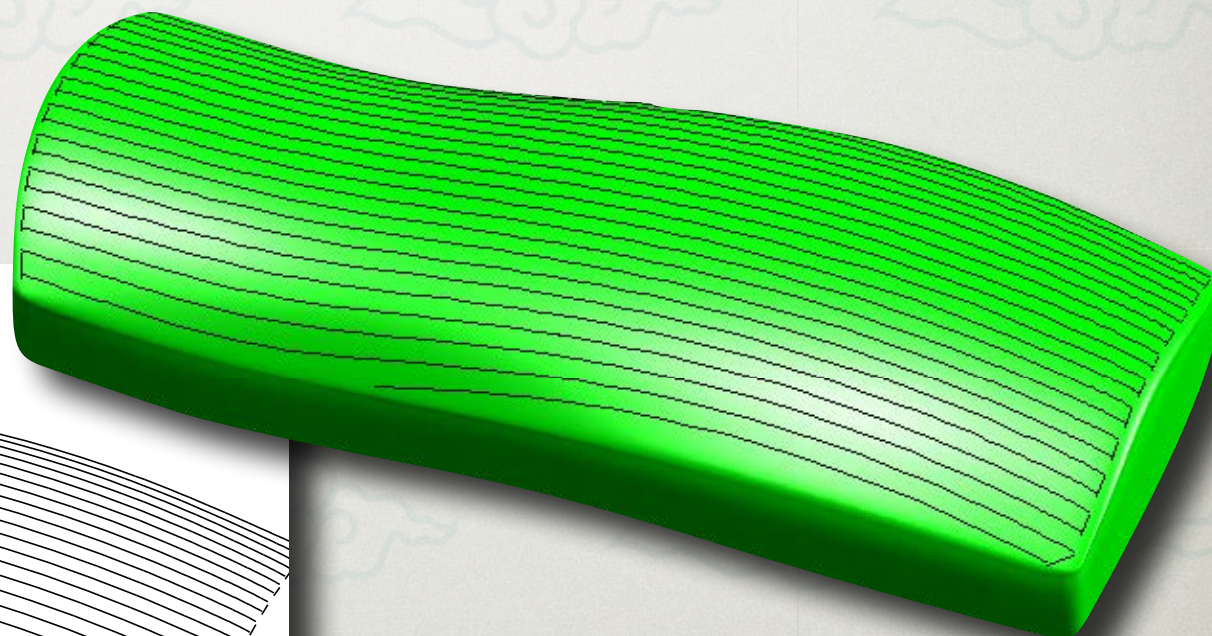
A. Gálvez, A. Iglesias: “A New Iterative Mutually-Coupled Hybrid GA-PSO Approach for Curve Fitting in Manufacturing”. **Applied Soft Computing** (I.F. 8.7), Vol.13, Issue 6, 1491-1504 (2013)







A. Gálvez, A. Iglesias: “A New Iterative Mutually-Coupled Hybrid GA-PSO Approach for Curve Fitting in Manufacturing”. **Applied Soft Computing** (I.F. 8.7), Vol. 13, Issue 6, 1491-1504 (2013)

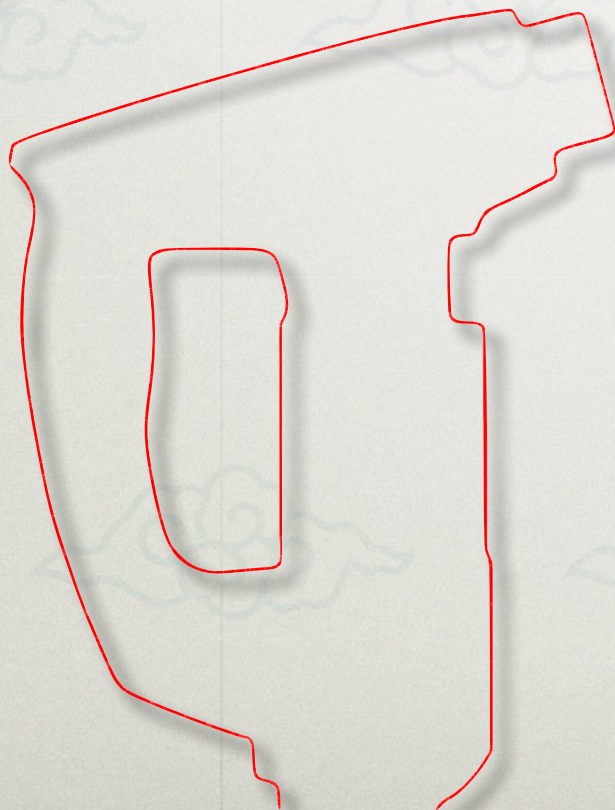




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Applied  
Soft  
Computing

A. Gálvez, A. Iglesias: *“A New Iterative Mutually-Coupled Hybrid GA-PSO Approach for Curve Fitting in Manufacturing”*. **Applied Soft Computing** (I.F. 8.7), Vol. 13, Issue 6, 1491-1504 (2013)

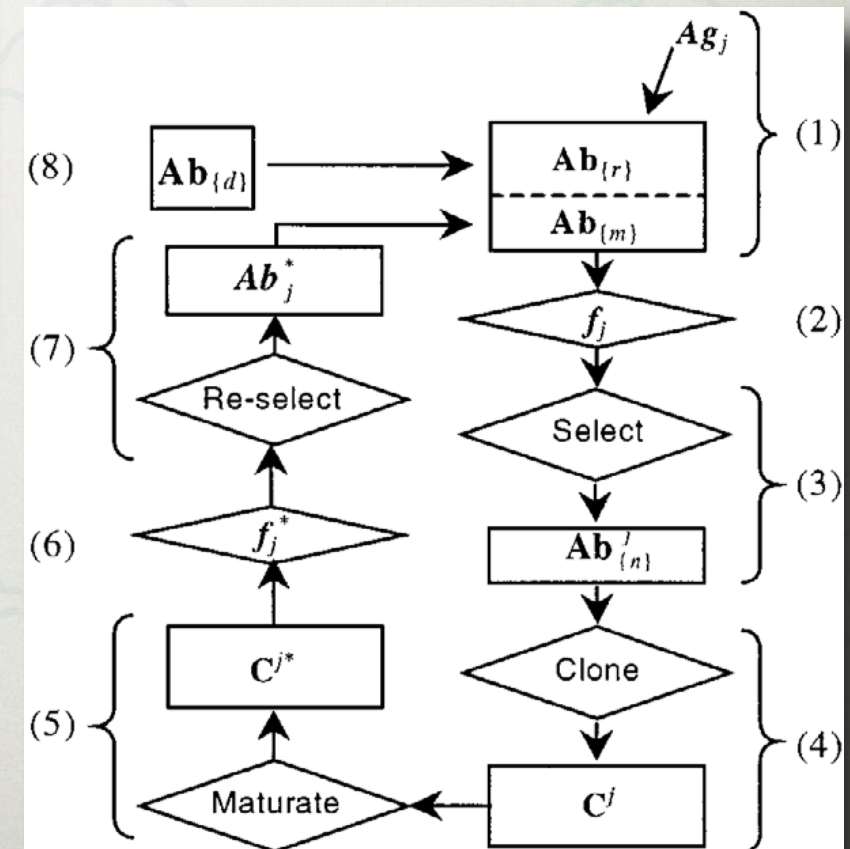




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A. Gálvez, A. Iglesias, A. Avila: *“Immunological-based approach for accurate fitting of 3D noisy data points with Bézier surfaces”*. **ICCS'2013 (CORE-A), 50-59 (2013)**

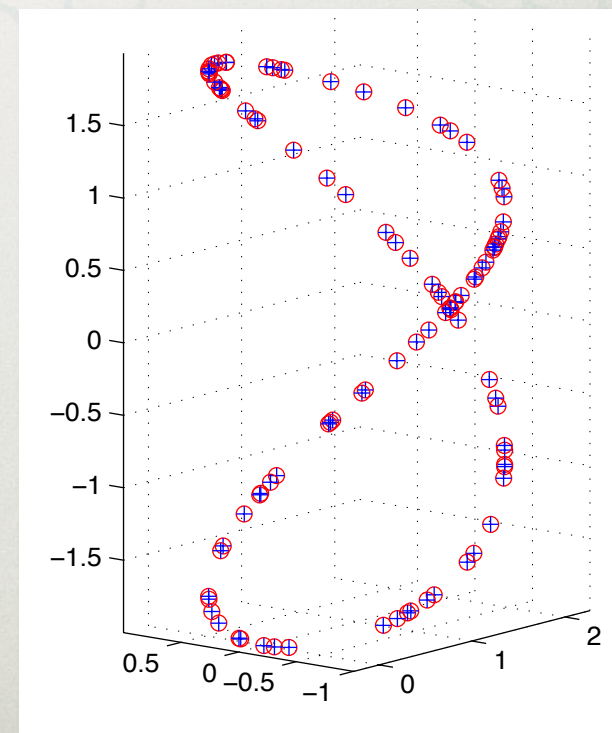
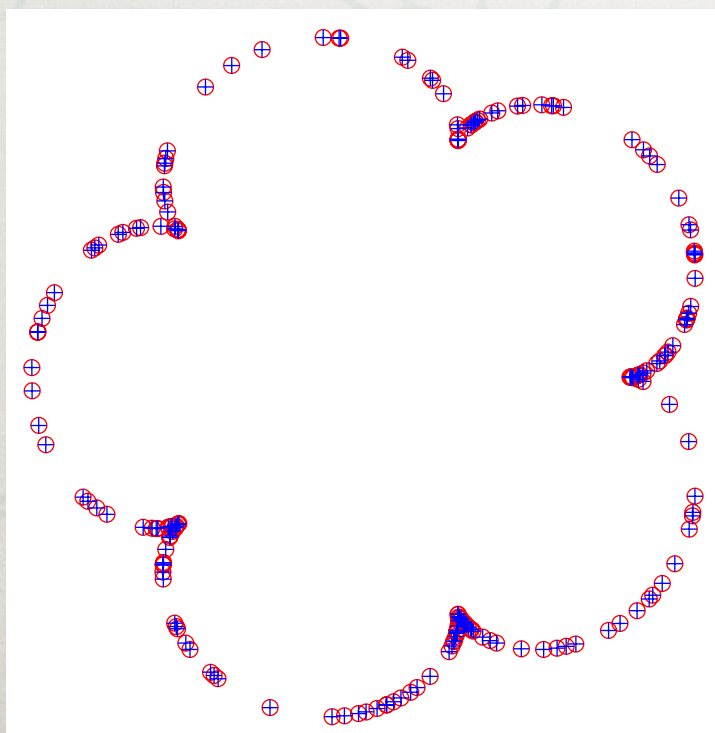




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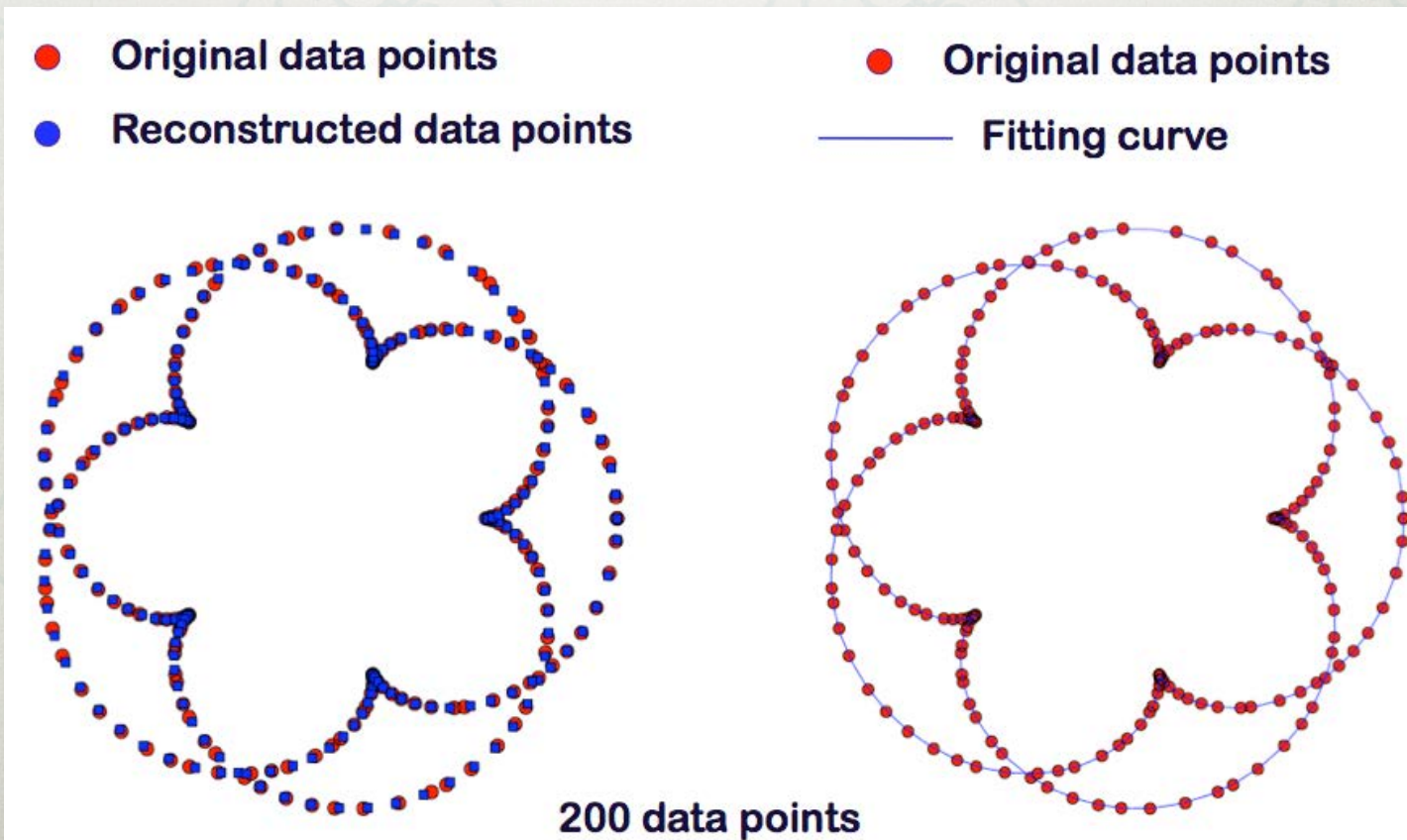
## A. Gálvez, A. Iglesias, L. Cabellos: “*Tabu Search-Based Method for Bézier Curve Parameterization*”. **Int. J. Software Eng. & Appl.**, Vol.7, Issue 5, 283-296 (2013)







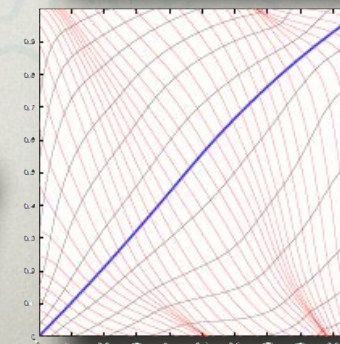
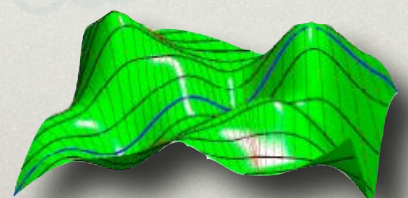
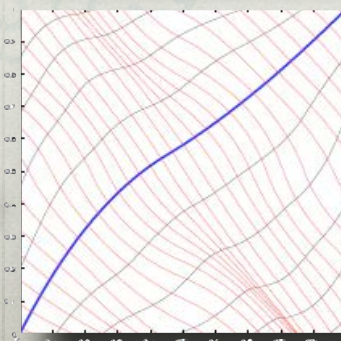
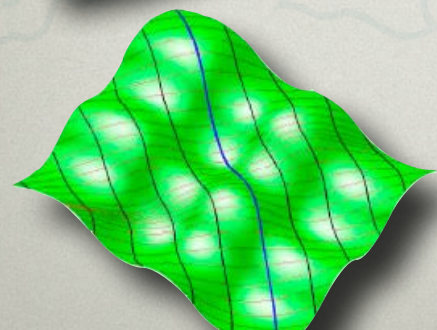
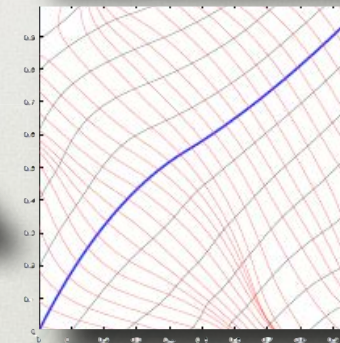
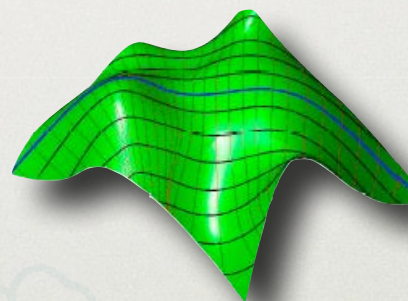
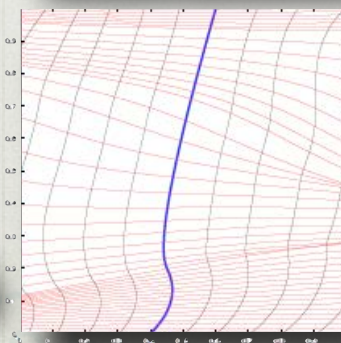
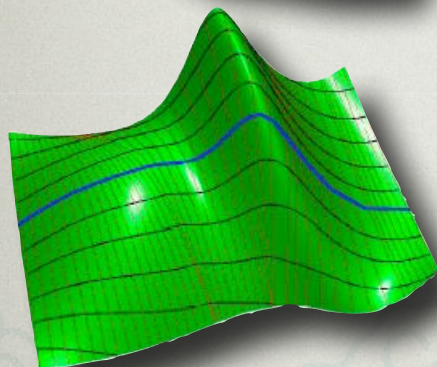
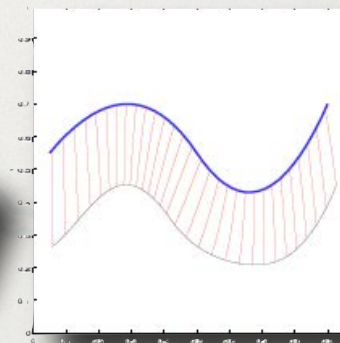
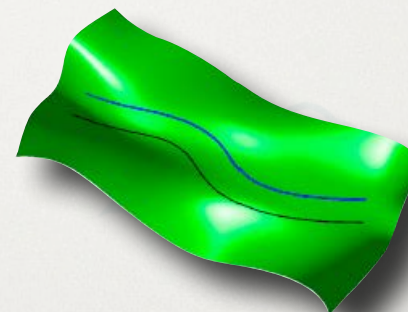
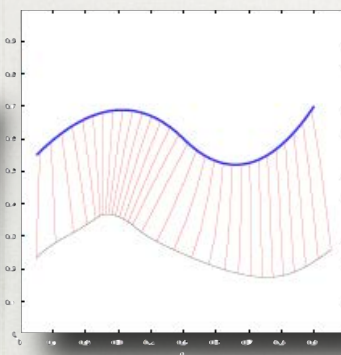
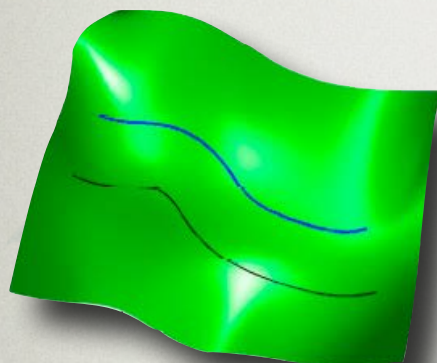
**A. Gálvez, A. Iglesias, L. Cabellos: “Firefly Algorithm for Explicit B-Spline Curve Fitting to Data Points”.  
Journal of Applied Mathematics (I.F. 0.834) (2013)**





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**A. Iglesias, A. Gálvez: “Computing parallel curves on parametric surfaces”.  
Applied Mathematical Modeling, (I.F. 5.0) Vol.38, 2398-2413 (2014)**





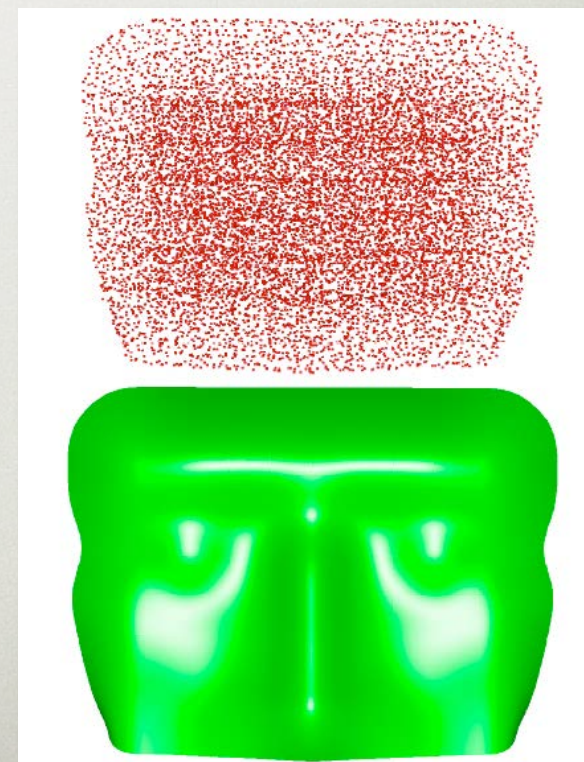
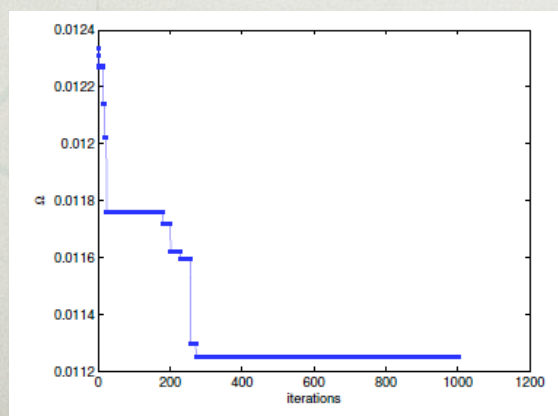
16<sup>th</sup> - 17<sup>th</sup> December 2023,

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A. Gálvez, A. Iglesias: *“Firefly Algorithm for Explicit B-Spline Curve Fitting to Data Points”*. **Mathematical Problems in Engineering (I.F. 1.383) (2013)**

A. Gálvez, A. Iglesias, A. Avila, C. Otero, R. Arias, C. Manchado: *“Elitist Clonal Selection Algorithm for Optimal Choice of Free Knots in B-spline Data Fitting”*. **Applied Soft Computing, (I.F. 8.7) (sub. April 2013)**

A. Gálvez, A. Iglesias: *“Hybrid Functional-Neural Approach for Surface Reconstruction”*. **Mathematical Problems in Engineering (I.F. 1.383) (2014)**

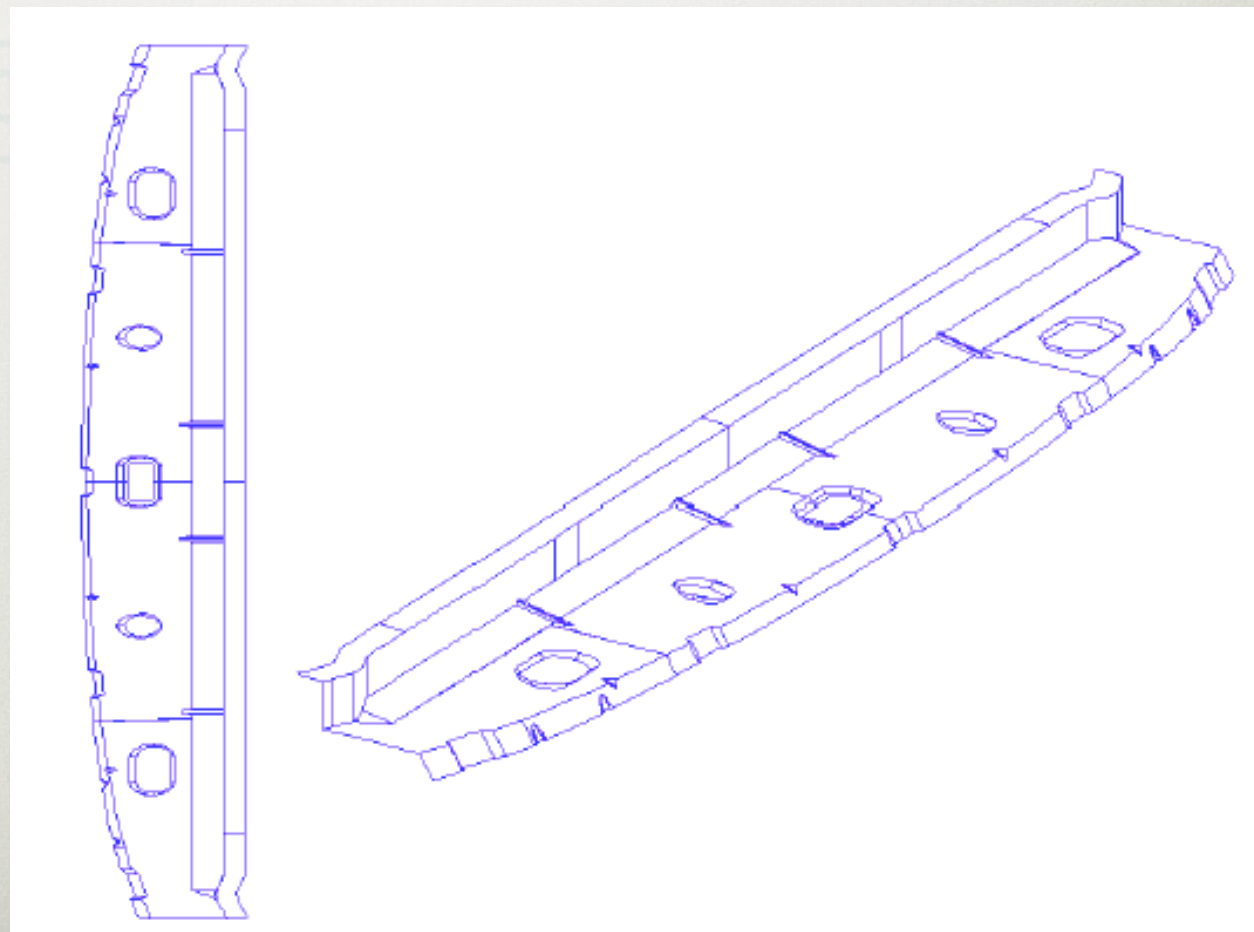
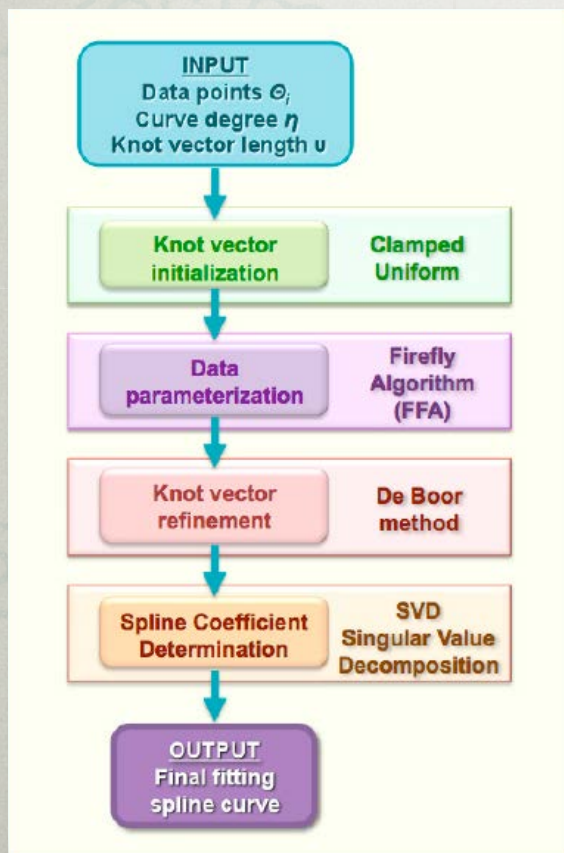




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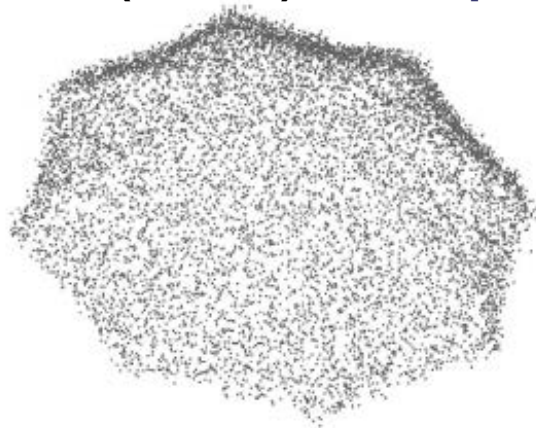
A. Gálvez, A. Iglesias: *“From Nonlinear Optimization to Convex Optimization Through Firefly Algorithm and Indirect Approach with Applications to CAD/CAM”*. **The Scientific World Journal (I.F. 1.730) (2013)**



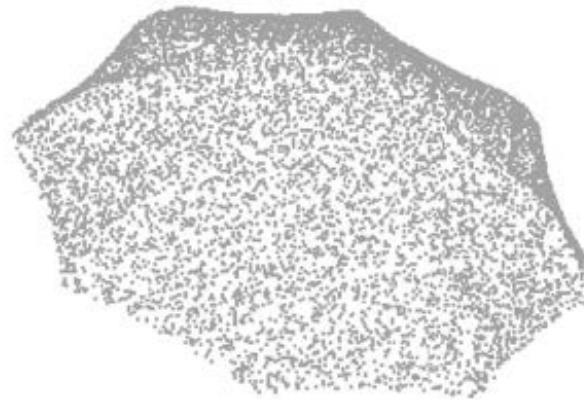


16<sup>th</sup> - 17<sup>th</sup> December 2023,  
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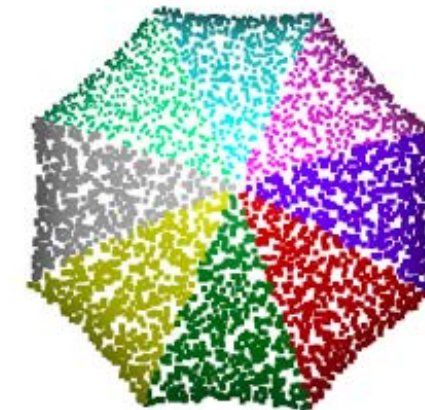
Z Zhu, A Zheng, A Iglesias, S Wang, Y Xia, E Chaudhry, L You, J Zhang: "*PDE patch-based surface reconstruction from point clouds*". **Journal of Computational Science (I.F. 3.3)**, 61, Paper 101647 (2022).



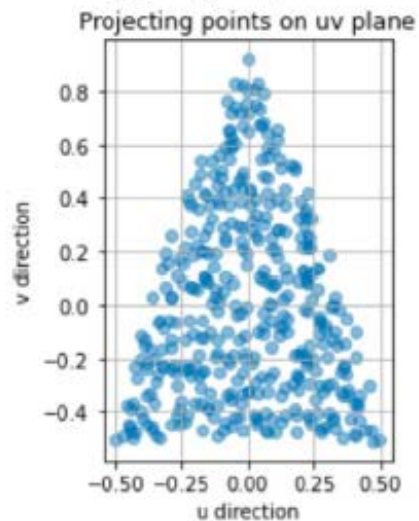
(a) Original point cloud data



(b) Preprocessing



(c) Segmentation



(d) Parameterization



(e) Patch fitting

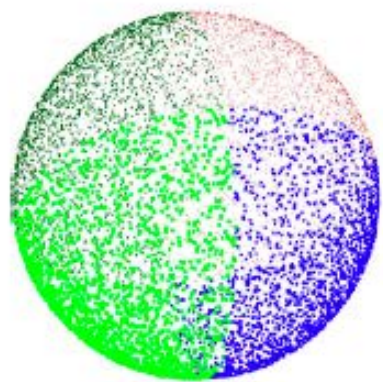


(f) Reconstructed surface

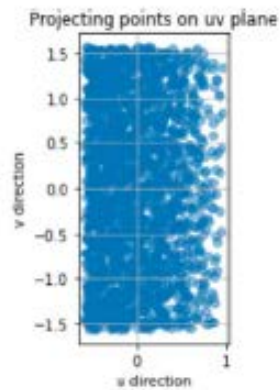


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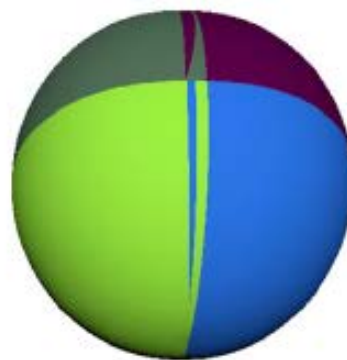
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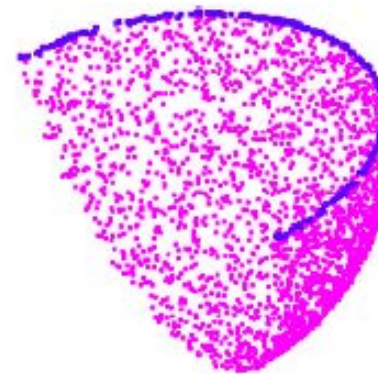
(a)



(b)



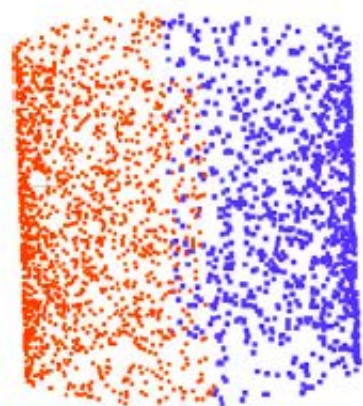
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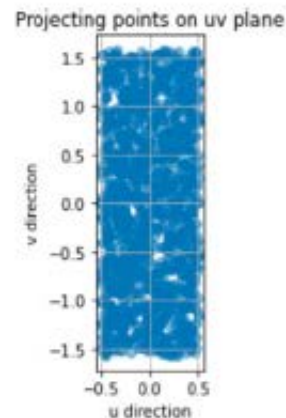
(d)



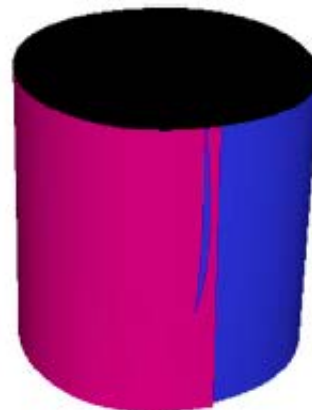
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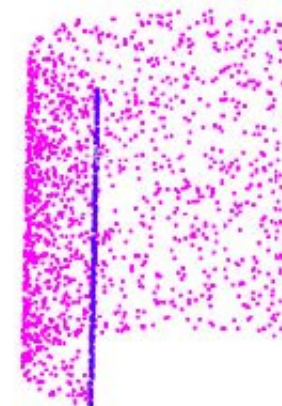
(a)



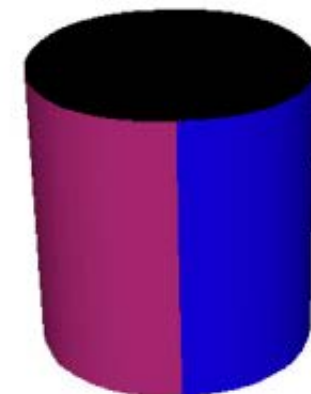
(b)



(c)



(d)

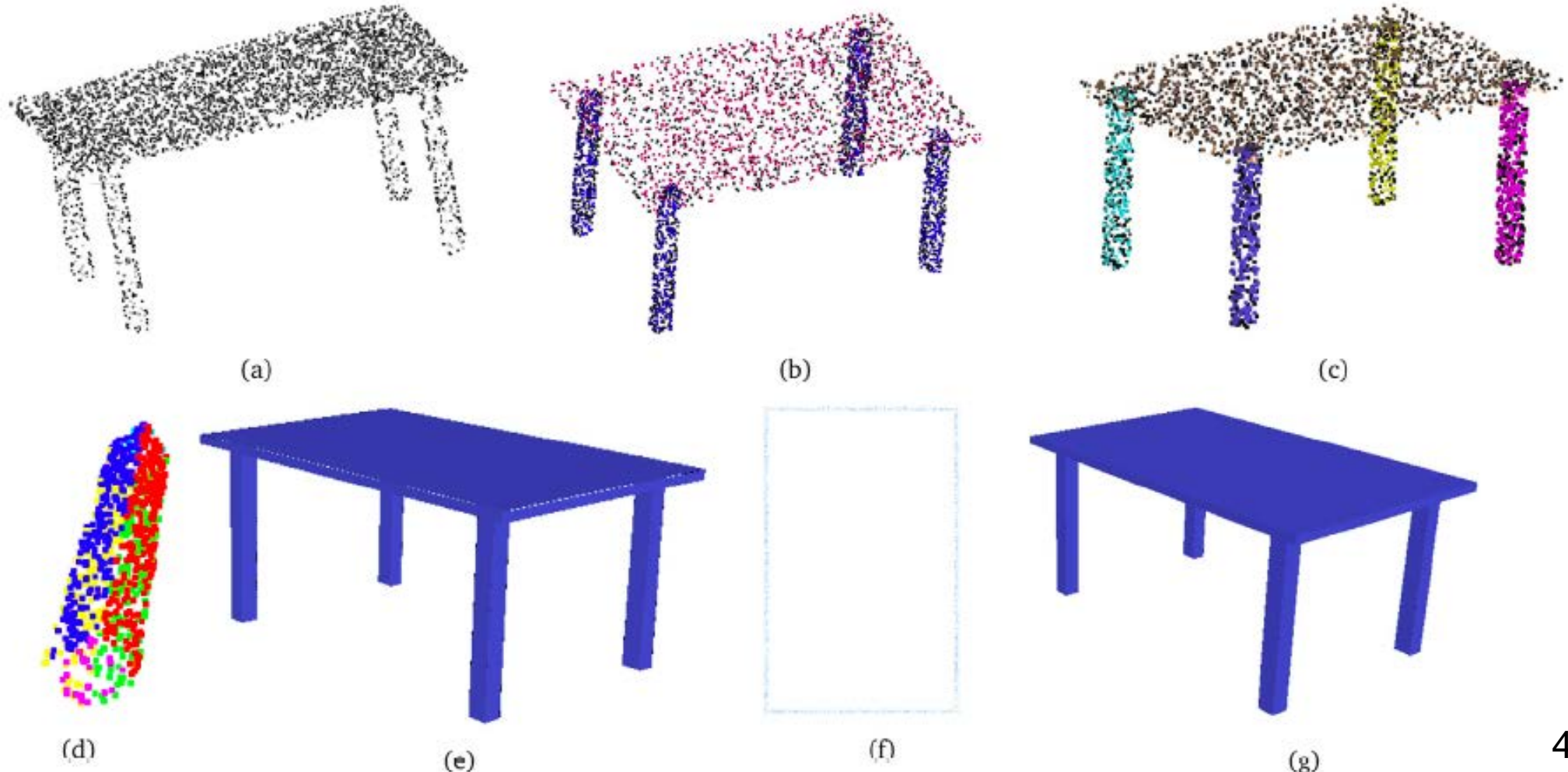


(e)



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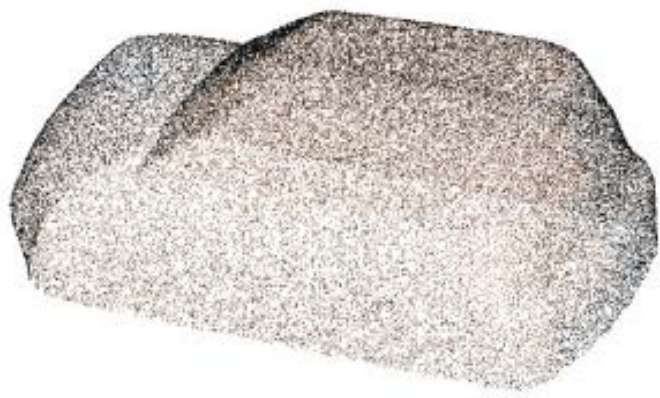
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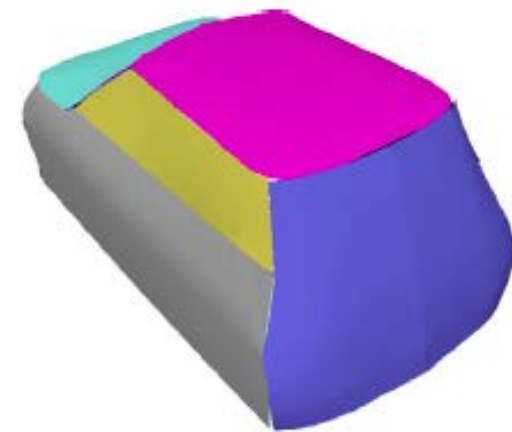
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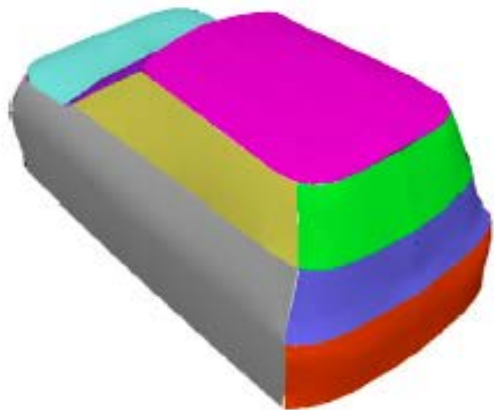
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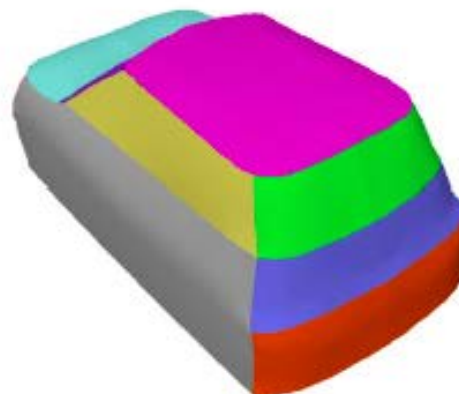
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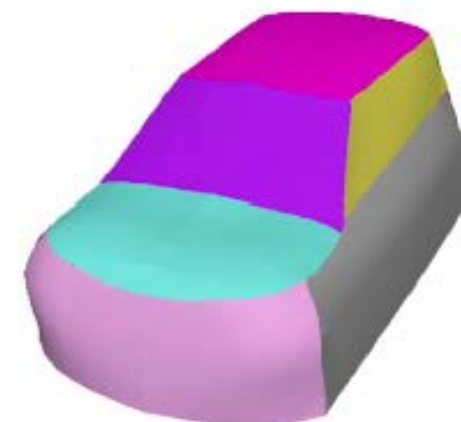
(c)



(d)



(e)

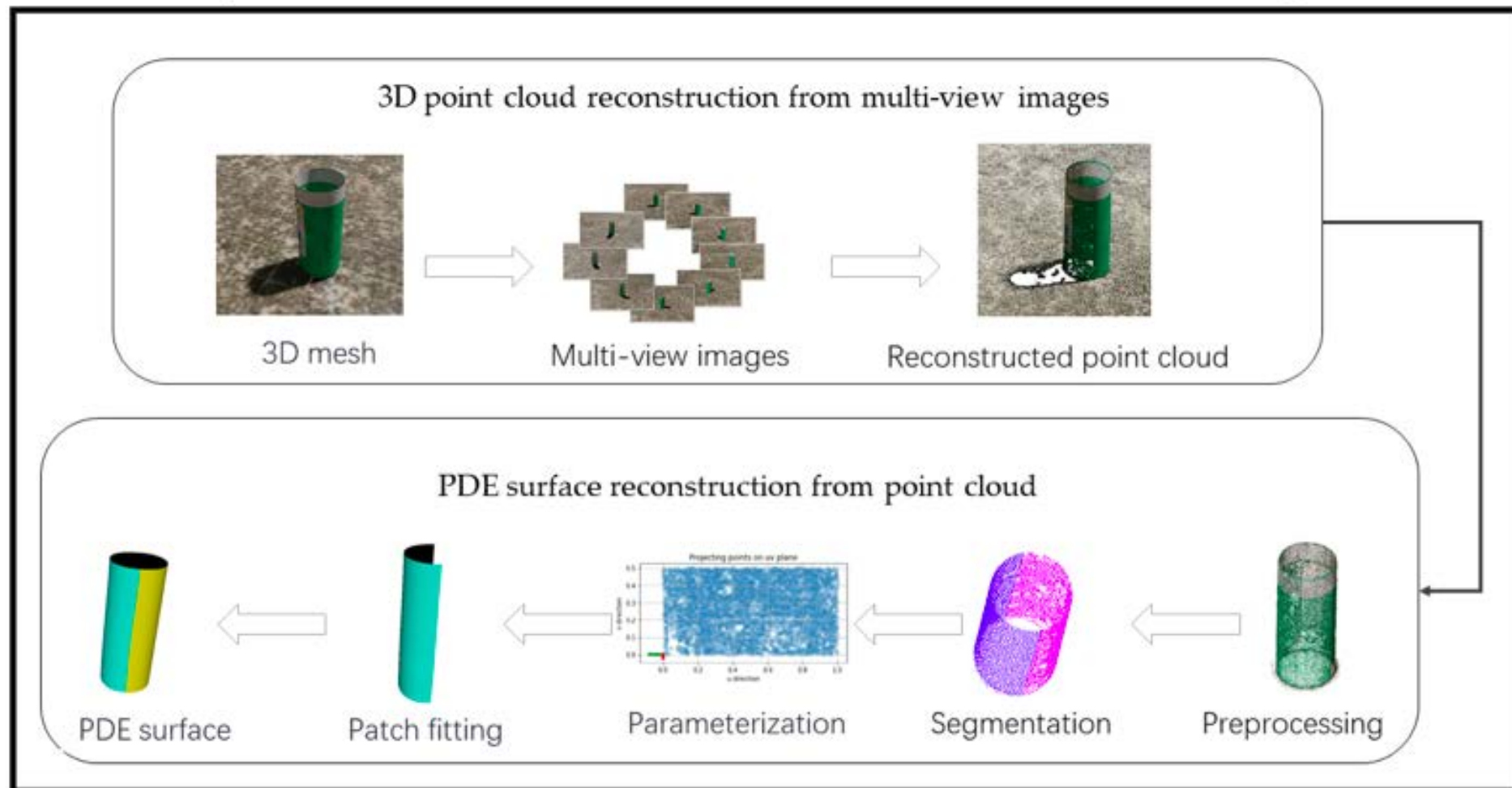


(f)



Zhu Z., Iglesias A., Zhou L., You L., Zhang J.J.: "PDE-Based 3D Surface Reconstruction from Multi-View 2D Images". **Mathematics** (I.F. 2.4), 10(4), Paper 542 (2022).

## Pipeline of PDE-surface reconstruction from multi-view images



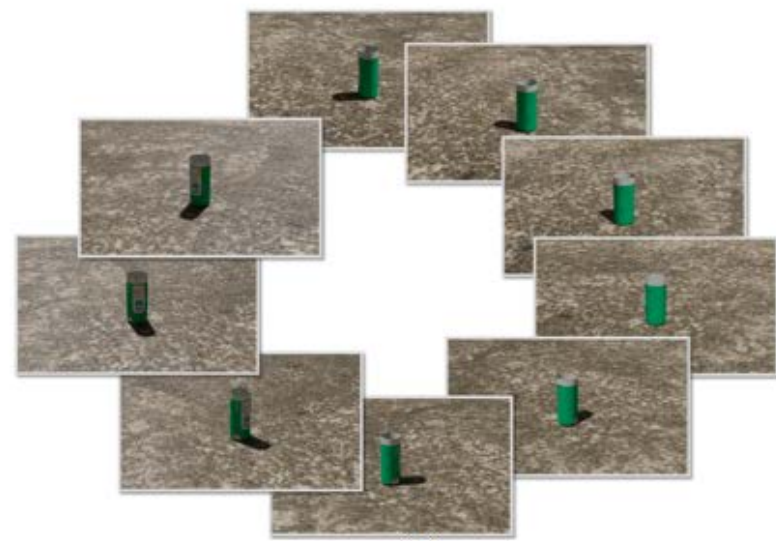


16<sup>th</sup> - 17<sup>th</sup> December 2023,  
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(a)



(b)



(a)



(b)



(c)



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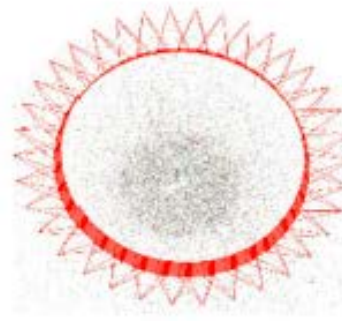


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(a)



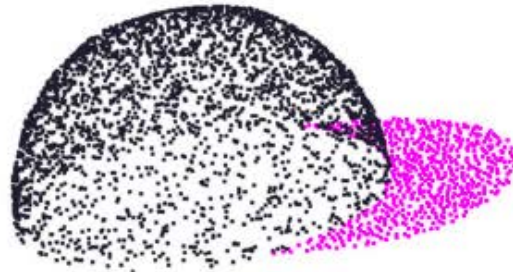
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(c)



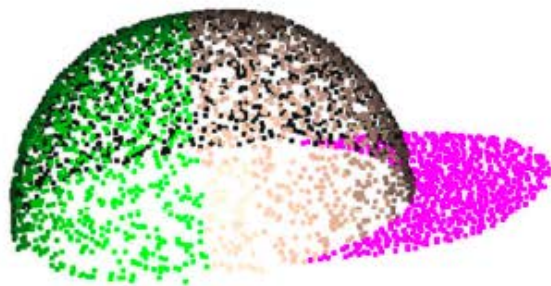
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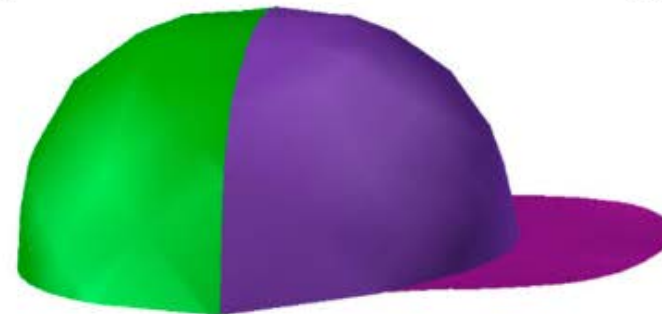
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(c)



(d)

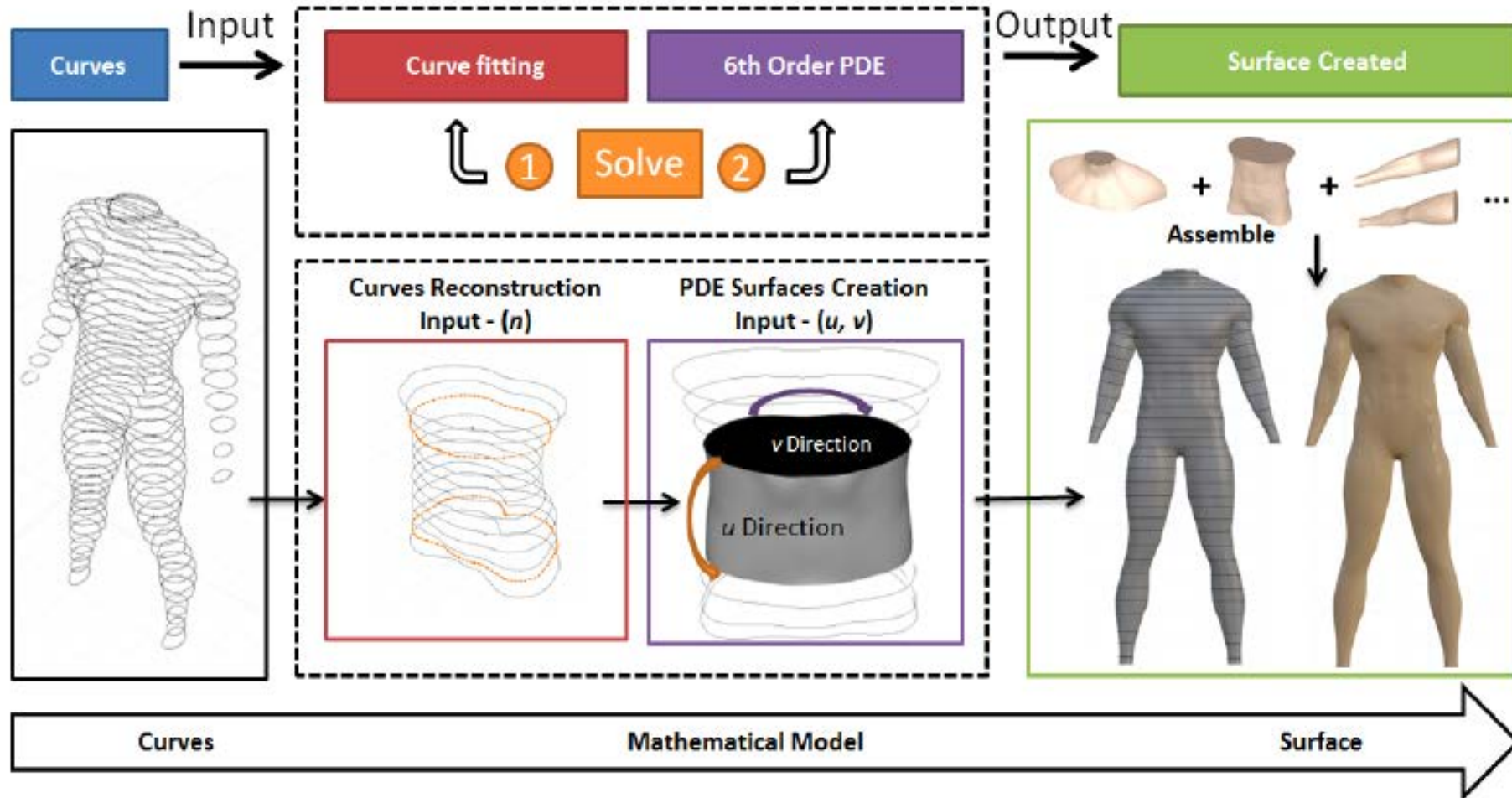


(e)



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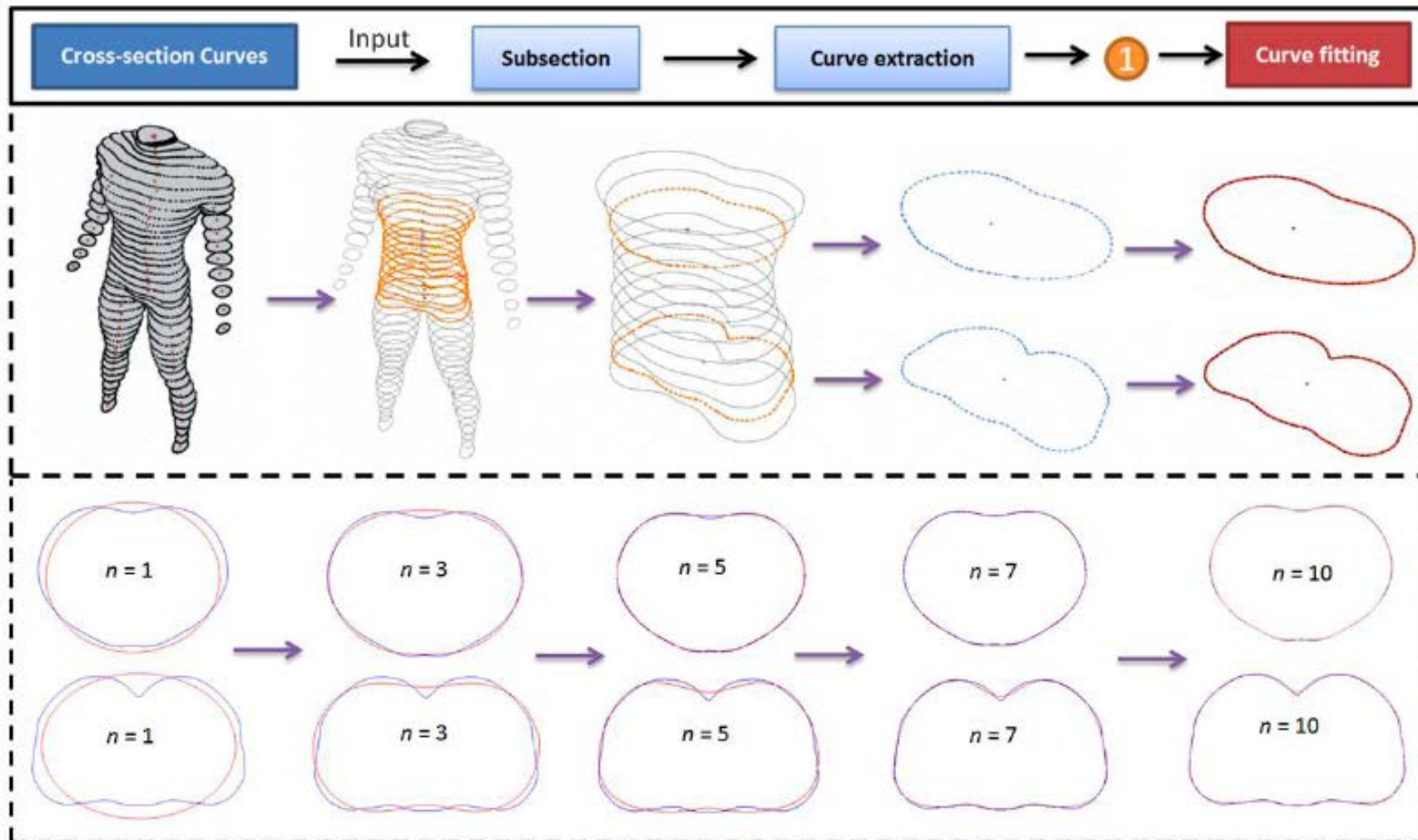
H. Fu, S. Bian, O. Li, J. Macey, A. Iglesias, E. Chaudhry, L. You, J.J. Zhang: "3D Modelling with  $C^2$  Continuous PDE Surface Patches". **Mathematics** (I.F. 2.4), 10(3), Paper 319 (2022).





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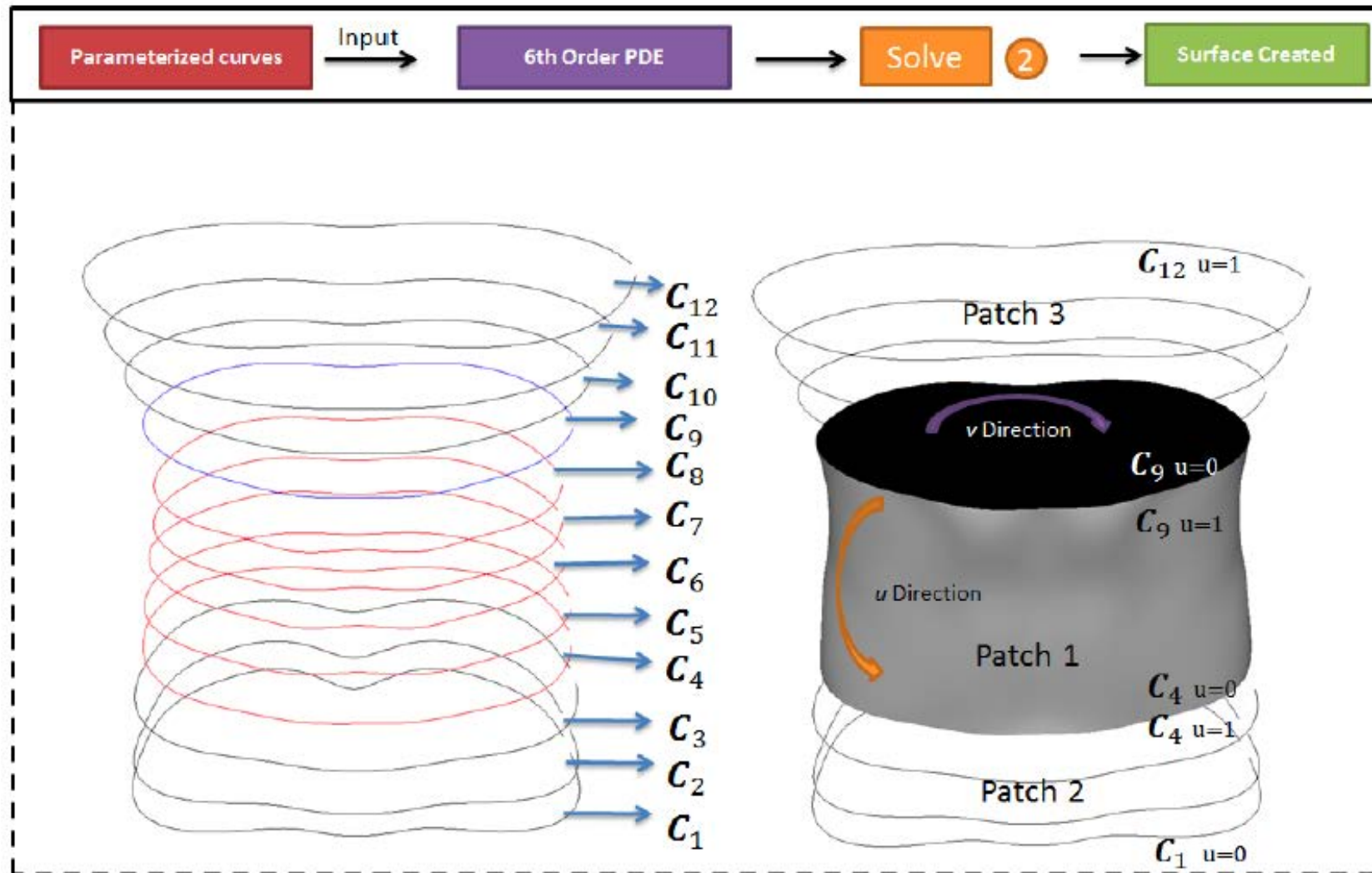
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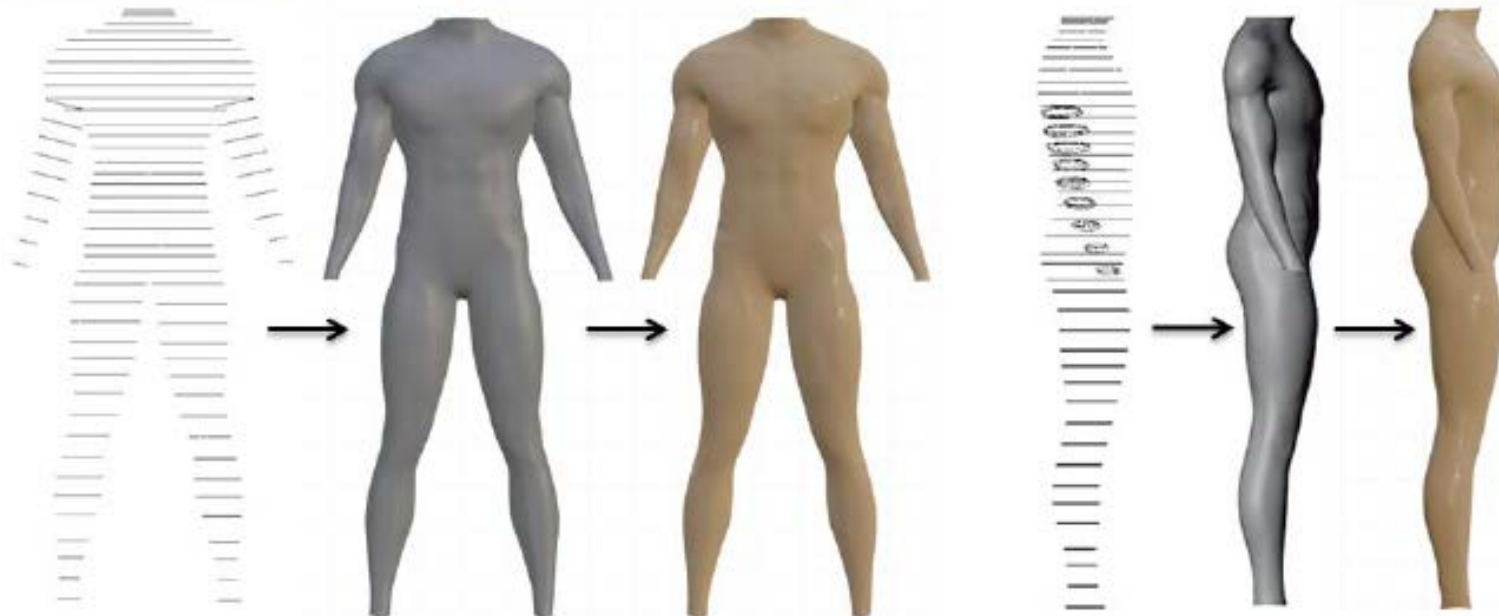
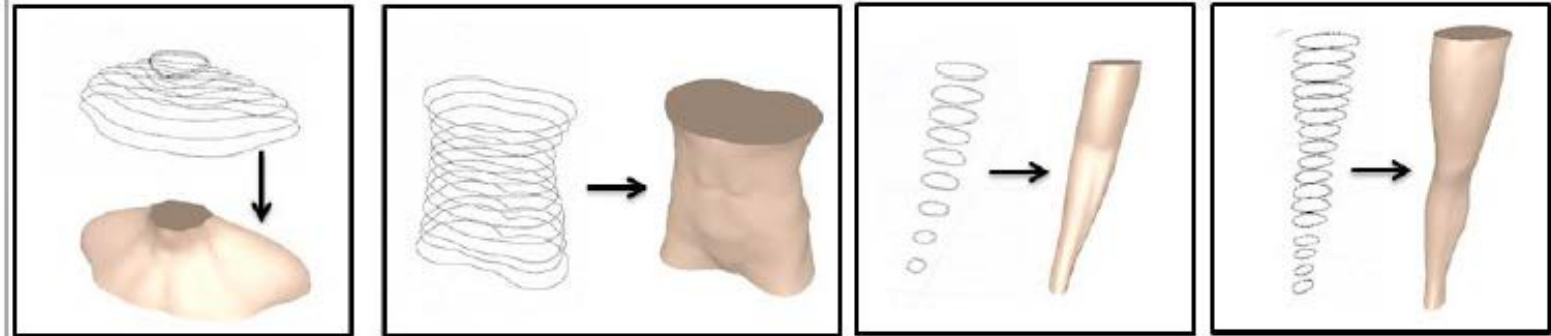
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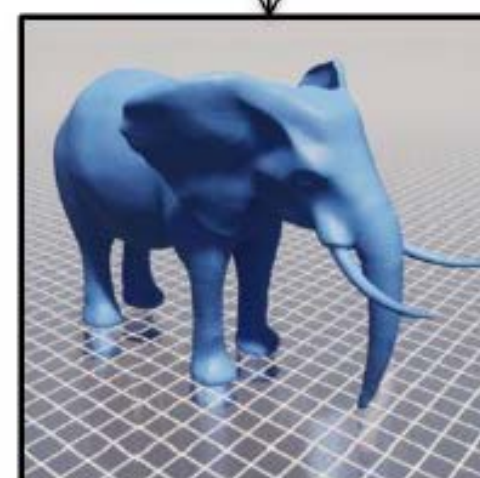
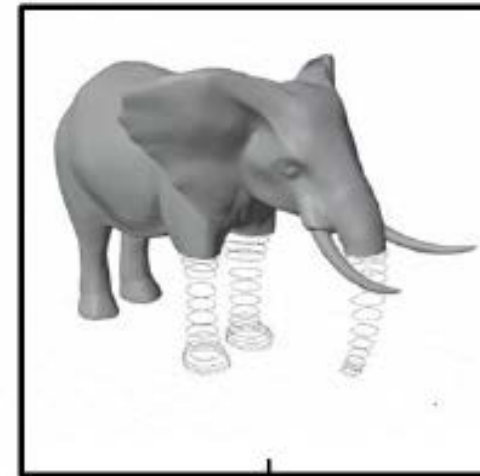
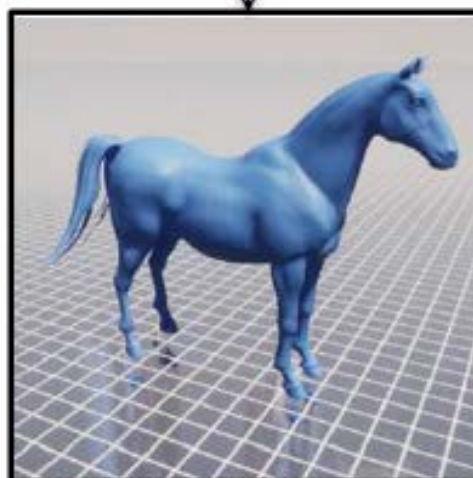
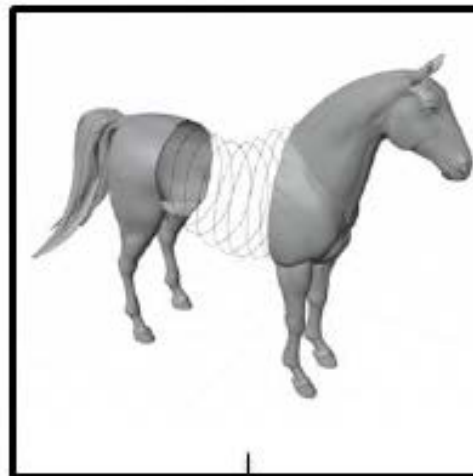
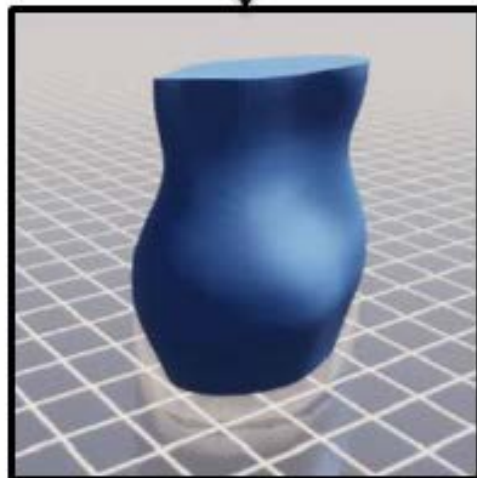
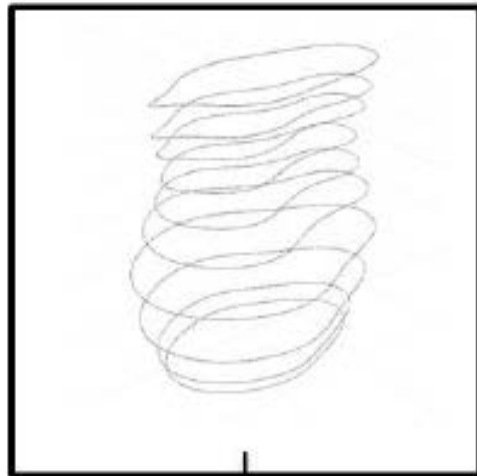
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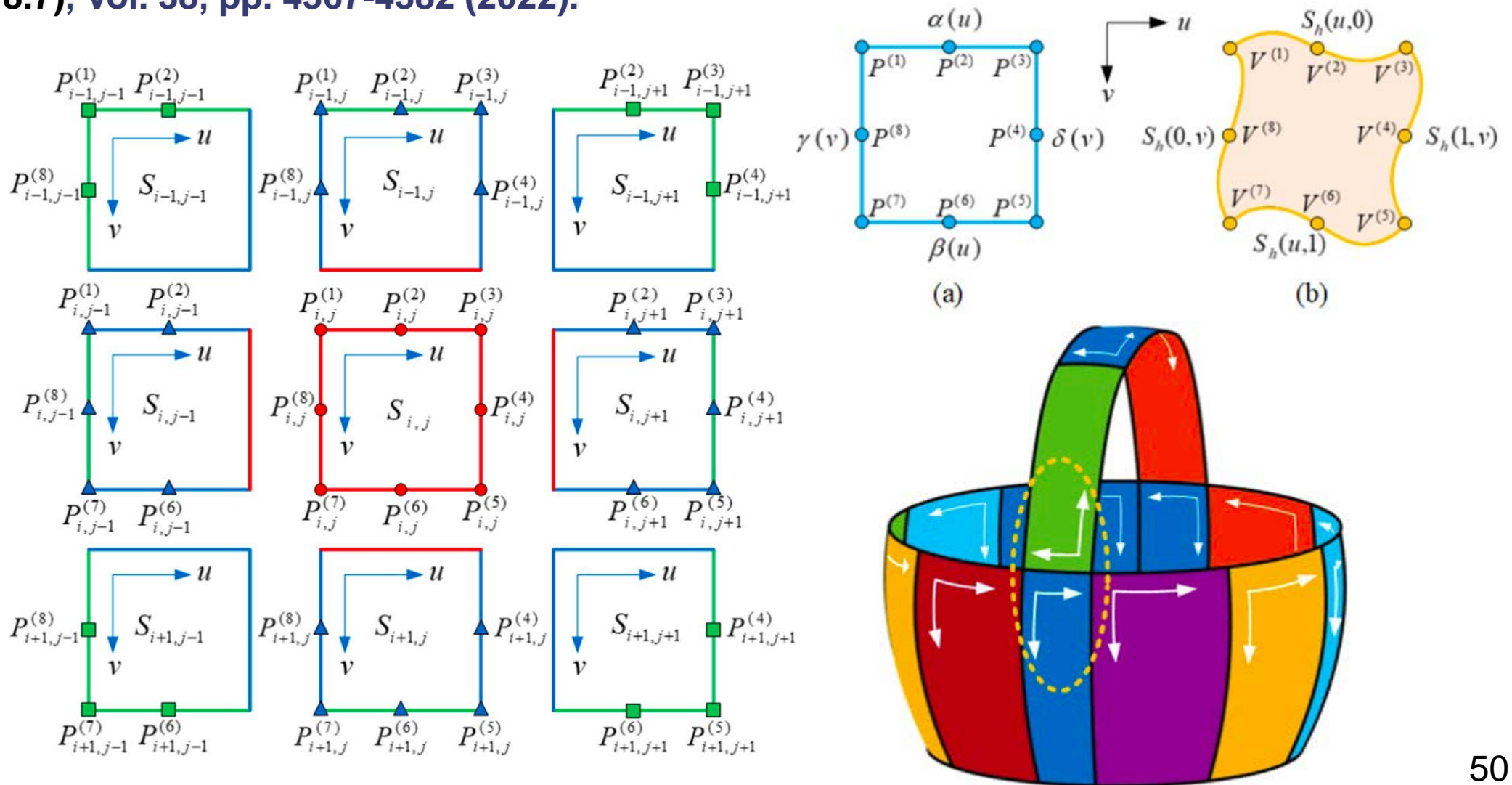
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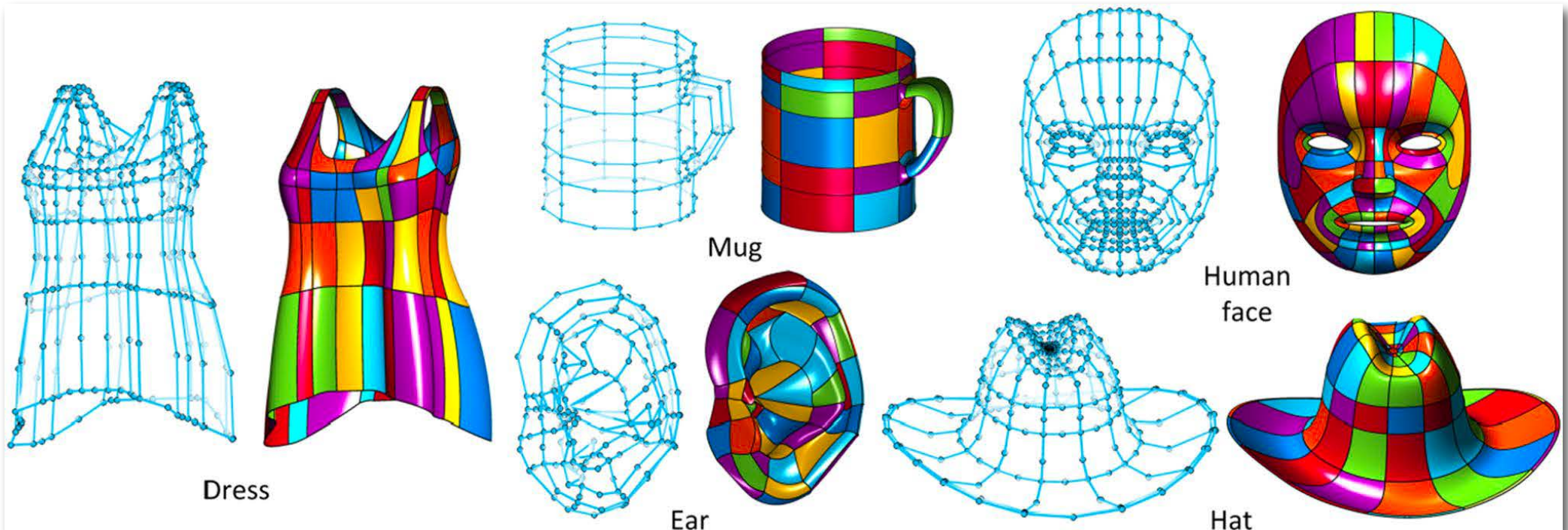
S. Wang, Y. Xia, L. You, H. Ugail, A. Carriazo, A. Iglesias, J.J. Zhang: "Interactive PDE patch-based surface modeling from vertex-frames". **Engineering with Computers (I.F. 8.7)**, Vol. 38, pp. 4367-4382 (2022).





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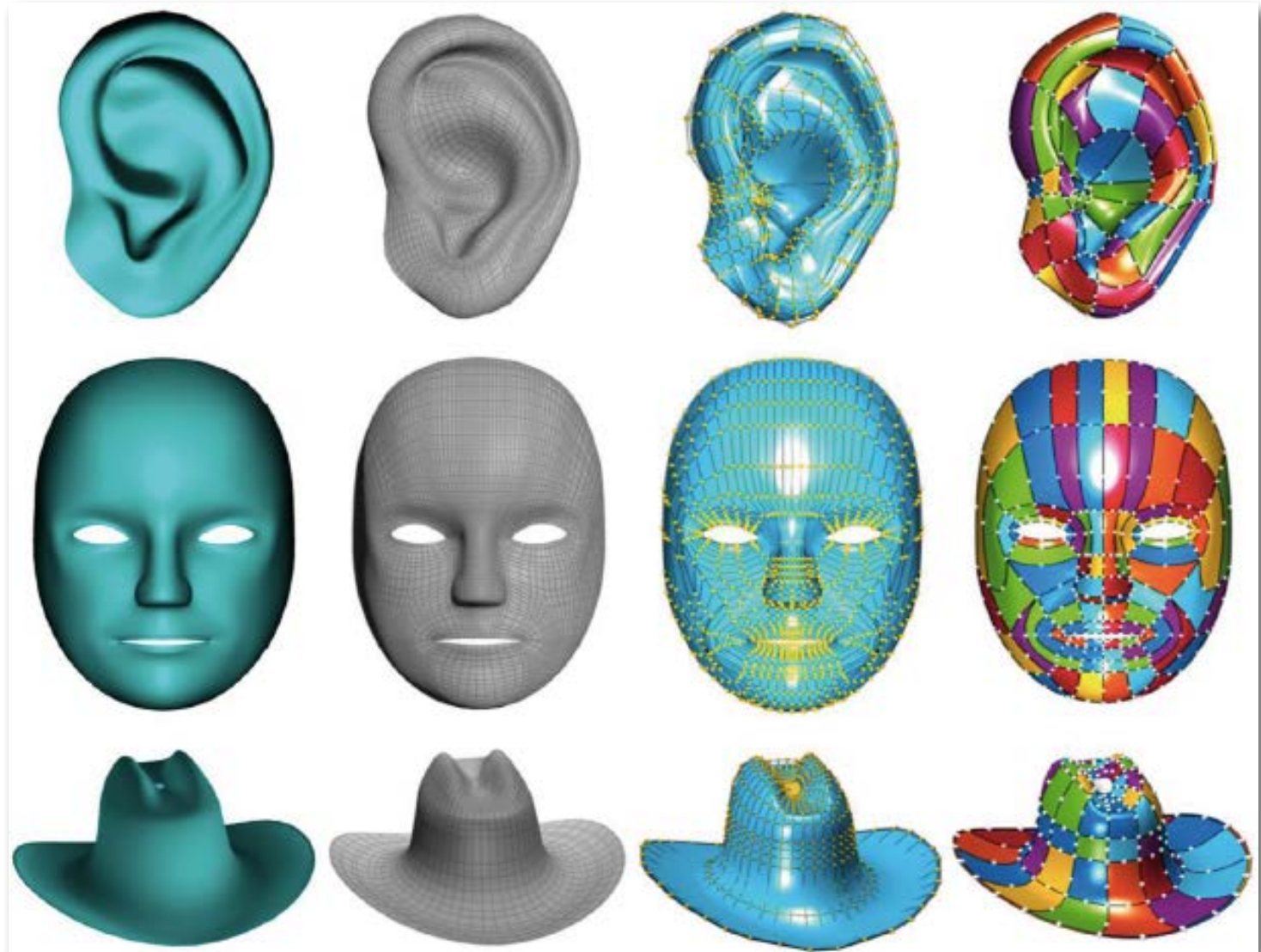


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	Vertices or control points		
	PO	NU	Ours
Dress	2996	1020	362
Mug	1275	460	168
Ear	1862	498	174
Hat	2256	900	312
Face	3701	963	336





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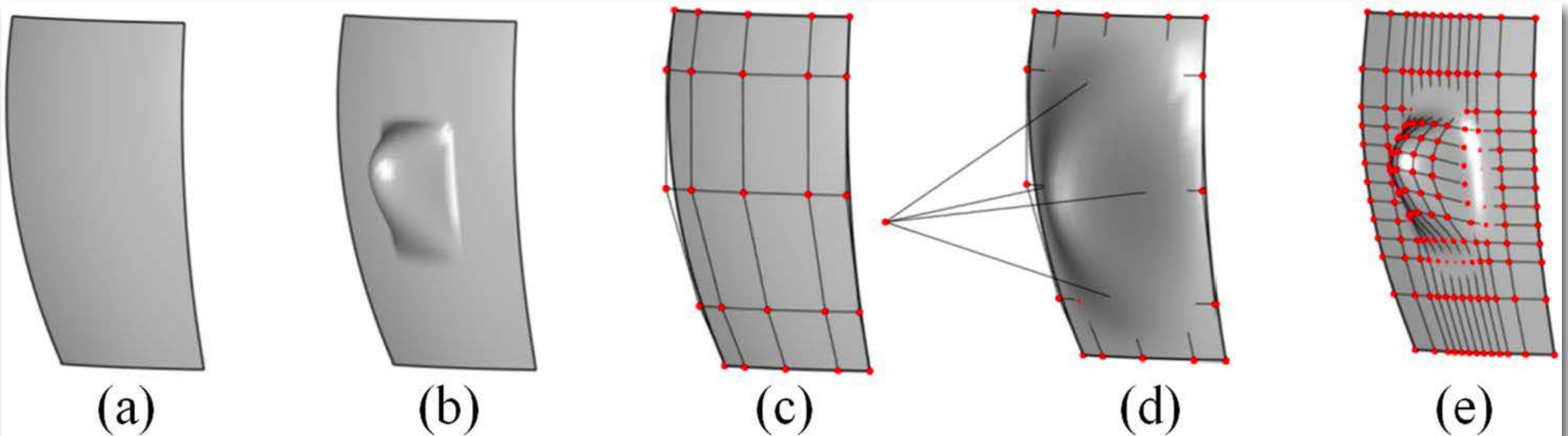
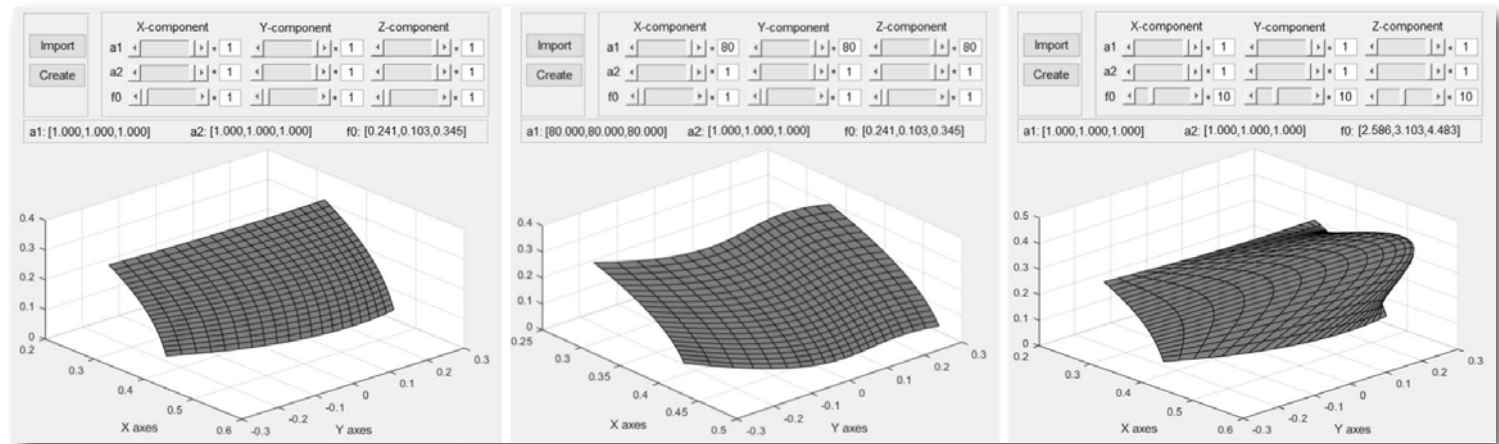
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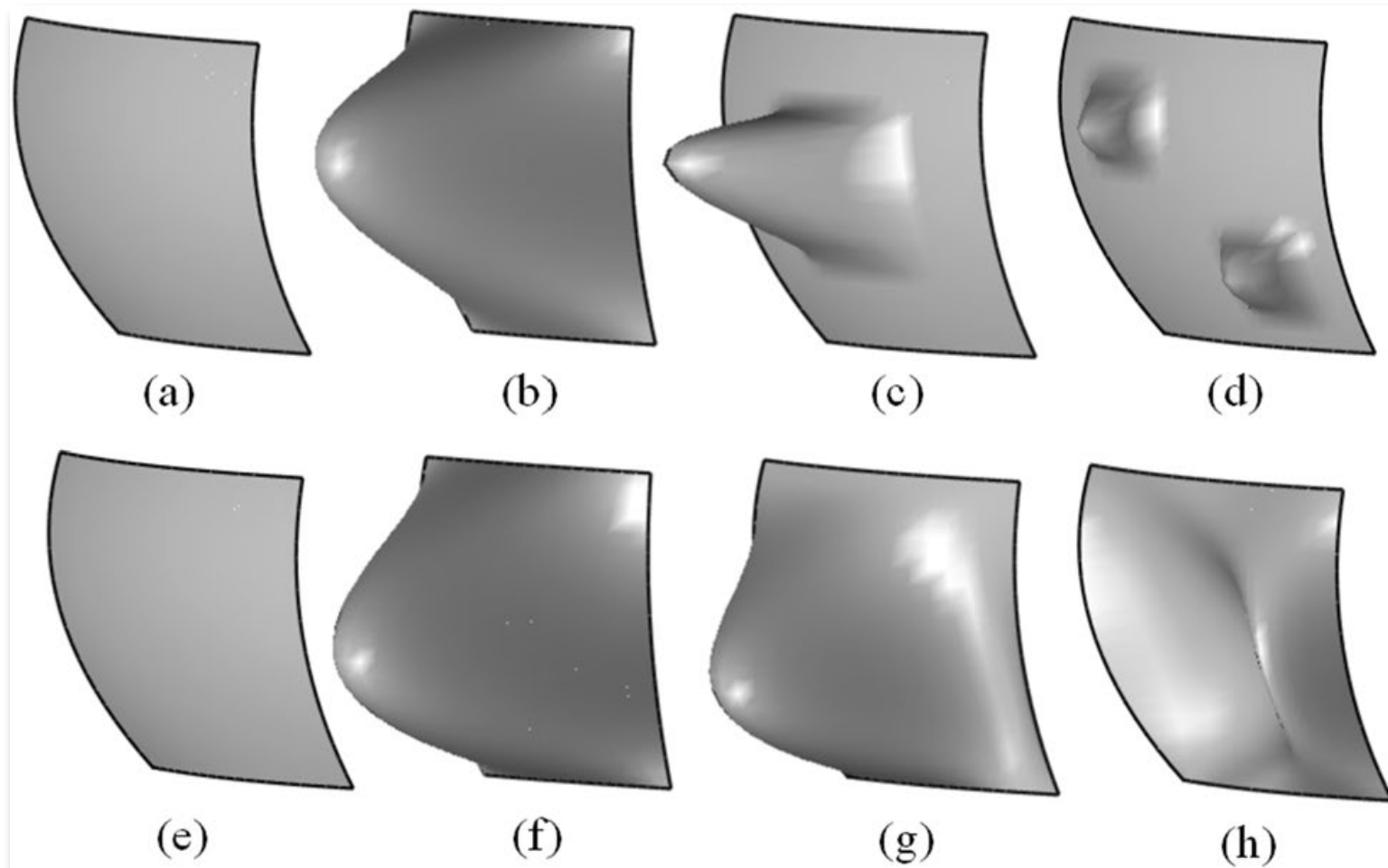
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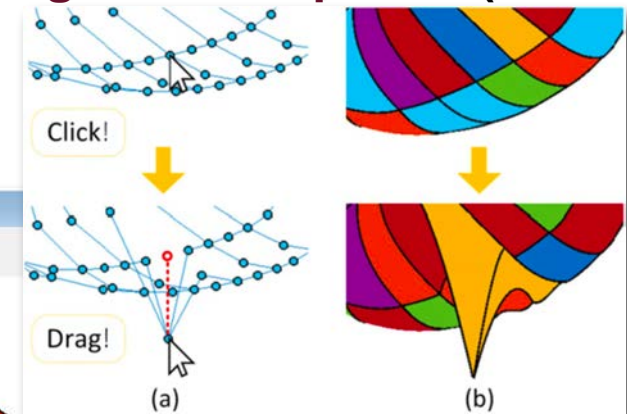
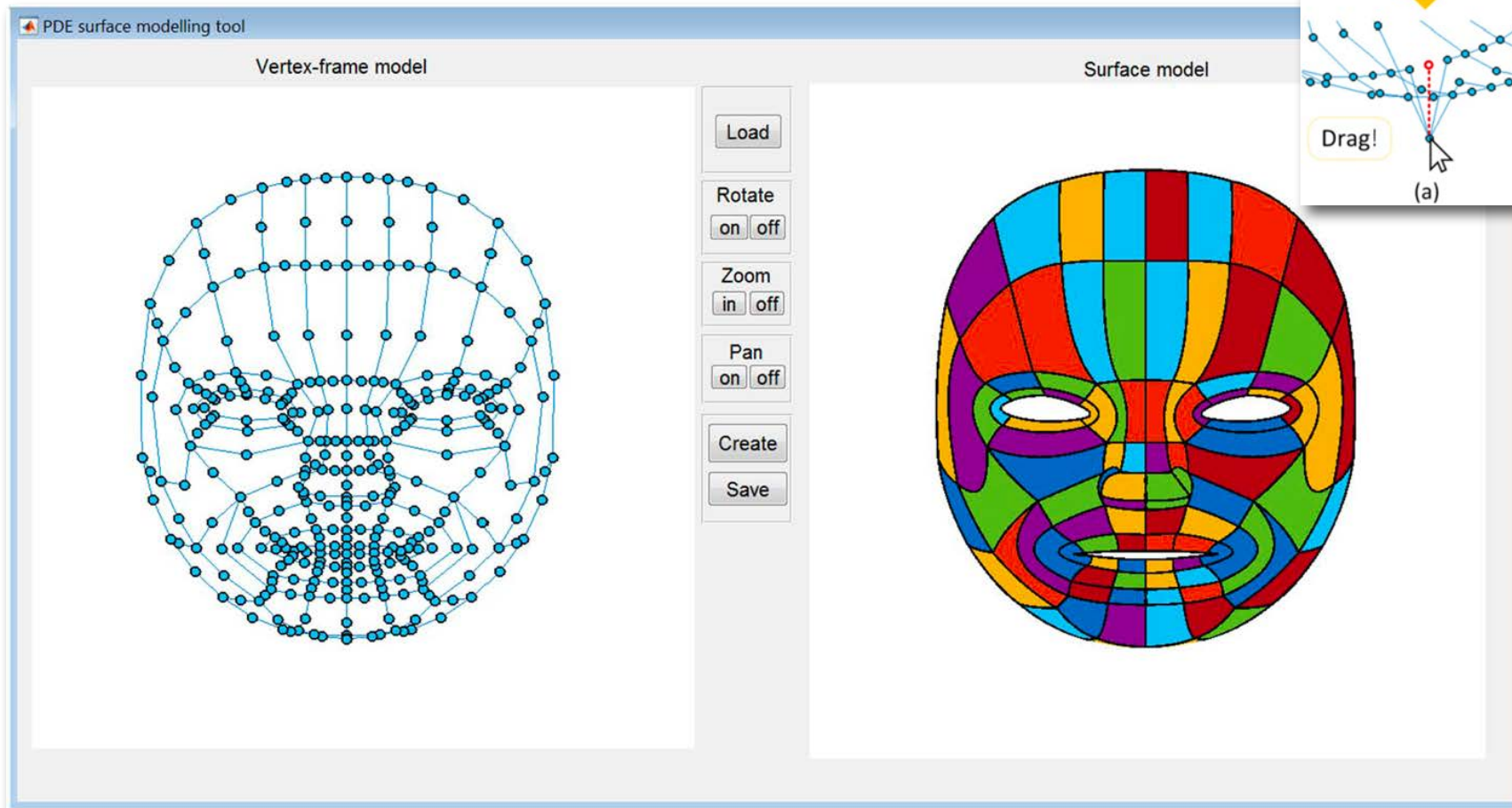
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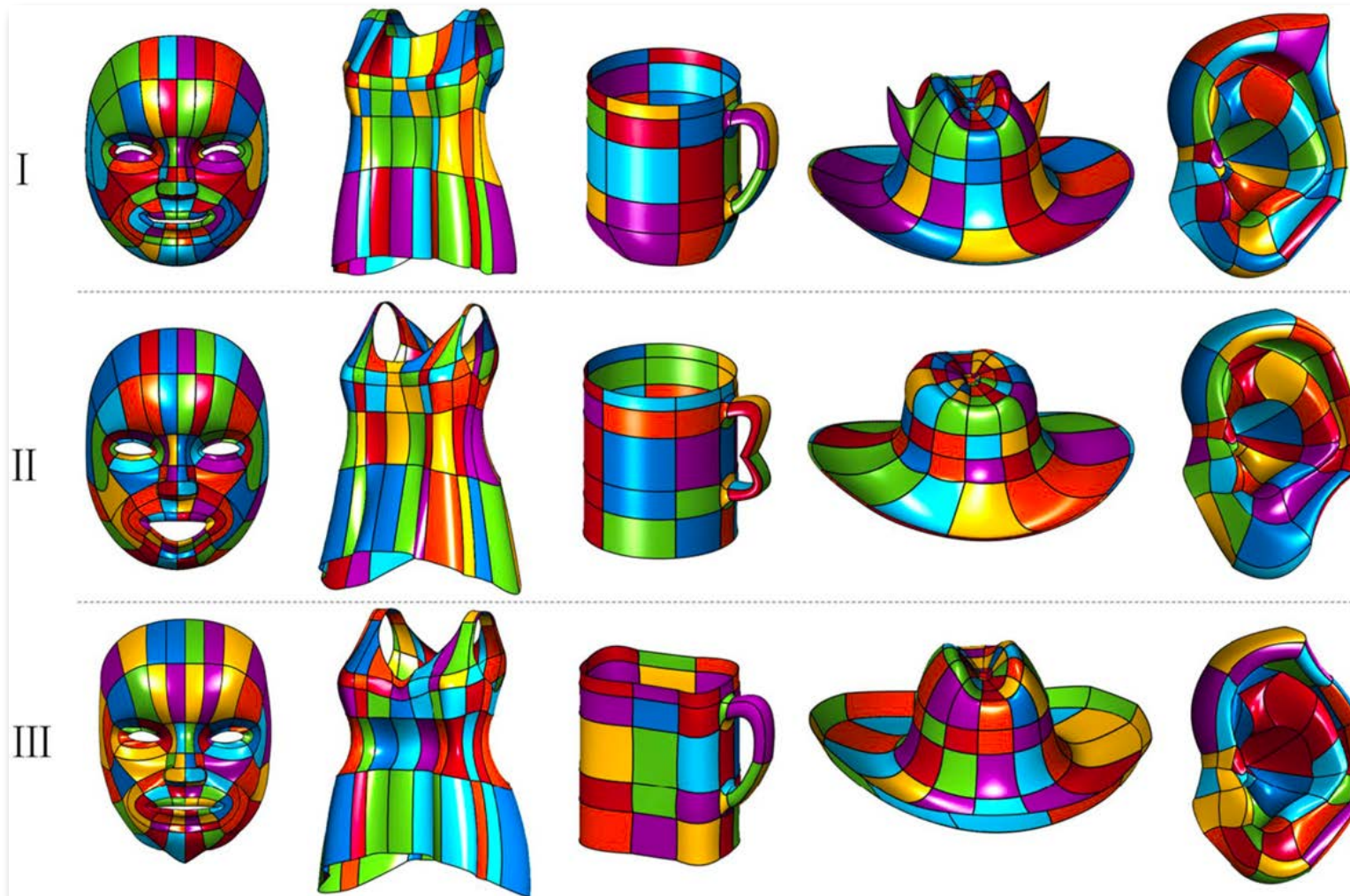
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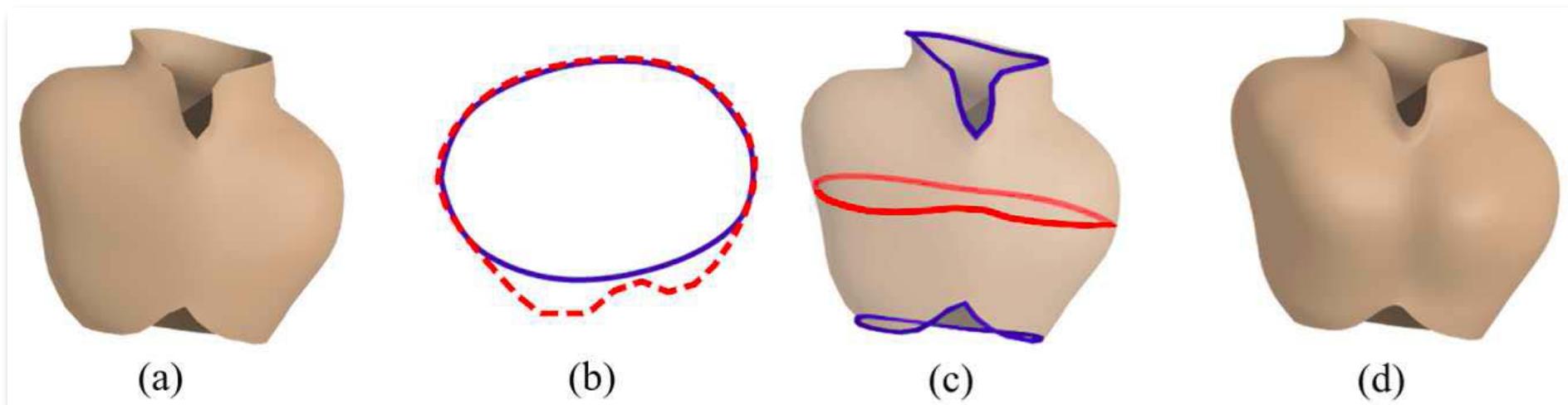
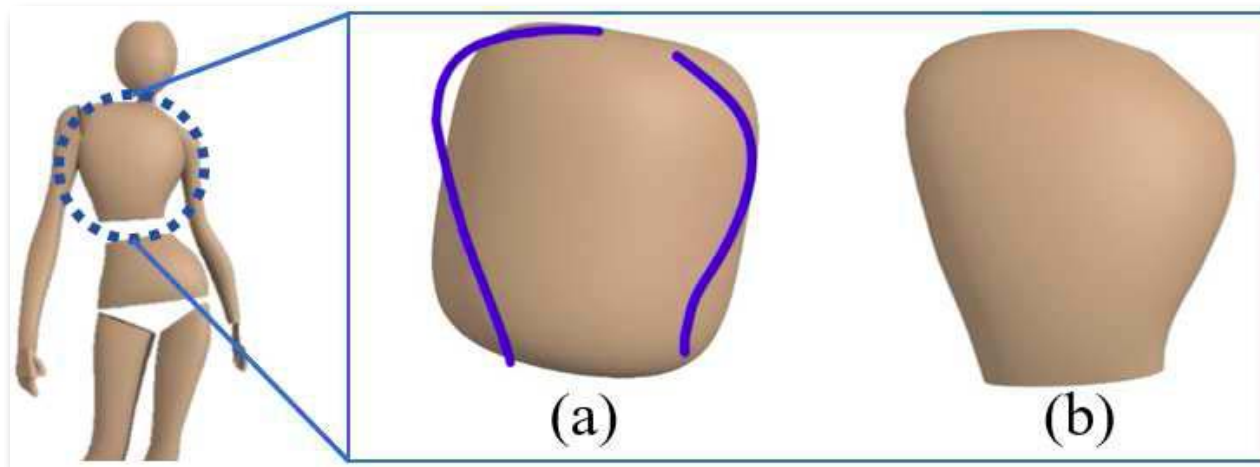






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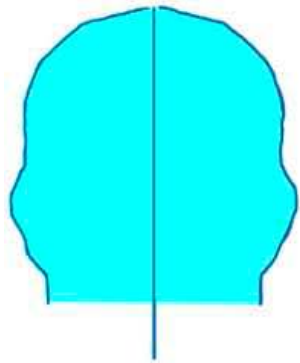
O. Li, H. Fu, S. Bian, X. Yang, X. Jin, A. Iglesias, A. Noreika, L. You, J.J. Zhang:  
"Character Modeling with Sketches and ODE-Based Shape Creation". **Numerical Mathematics: Theory, Methods and Applications**, (I.F. 1.3) Vol. 16, pp. 720-751 (2023).



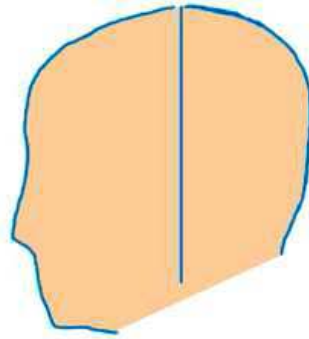


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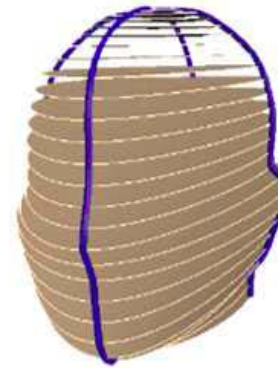
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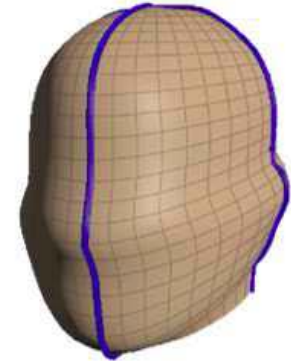
(a)



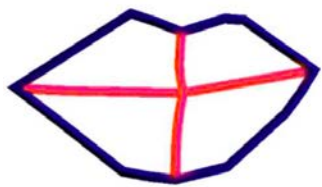
(b)



(c)



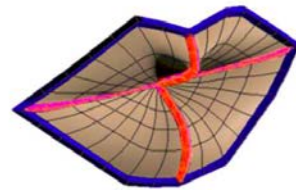
(d)



(a)



(b)



(c)



(a)



(b)



(c)



(d)



(e)



(f)

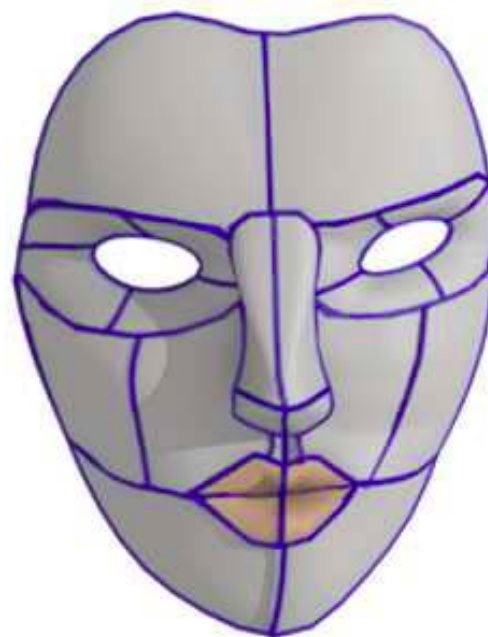


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(a)



(b)



(c)



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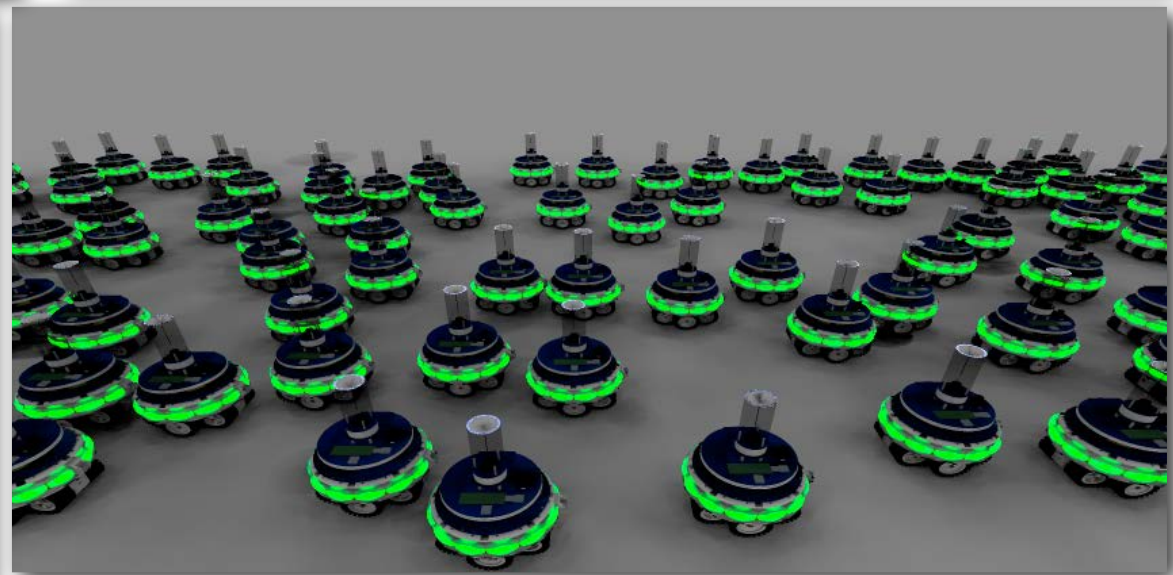
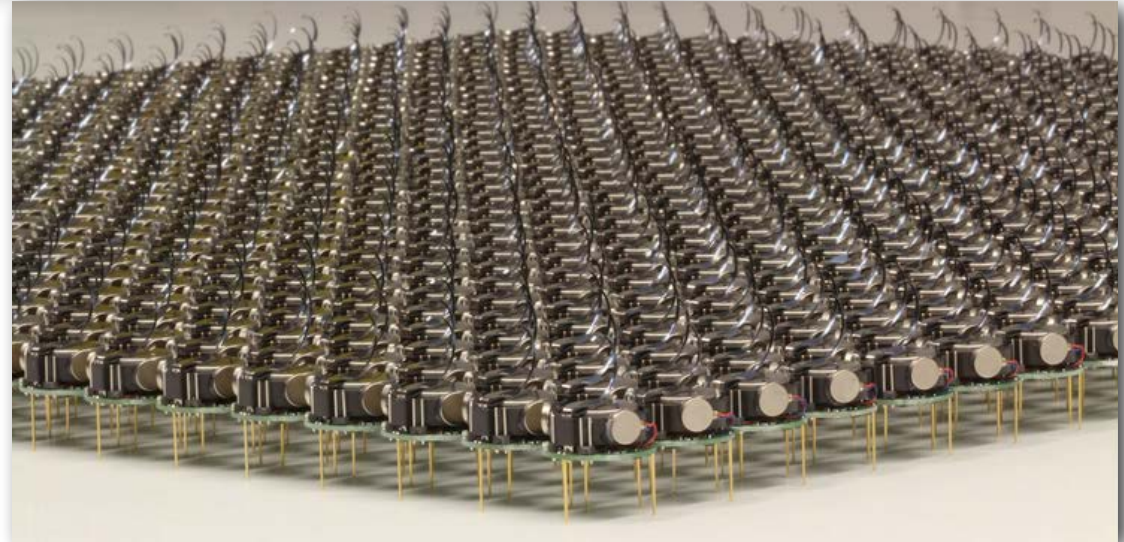
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## Swarm Robotics





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## Main components: single-board micro-controller

(small, affordable, reasonable  
computing power)

ultrasound sensors

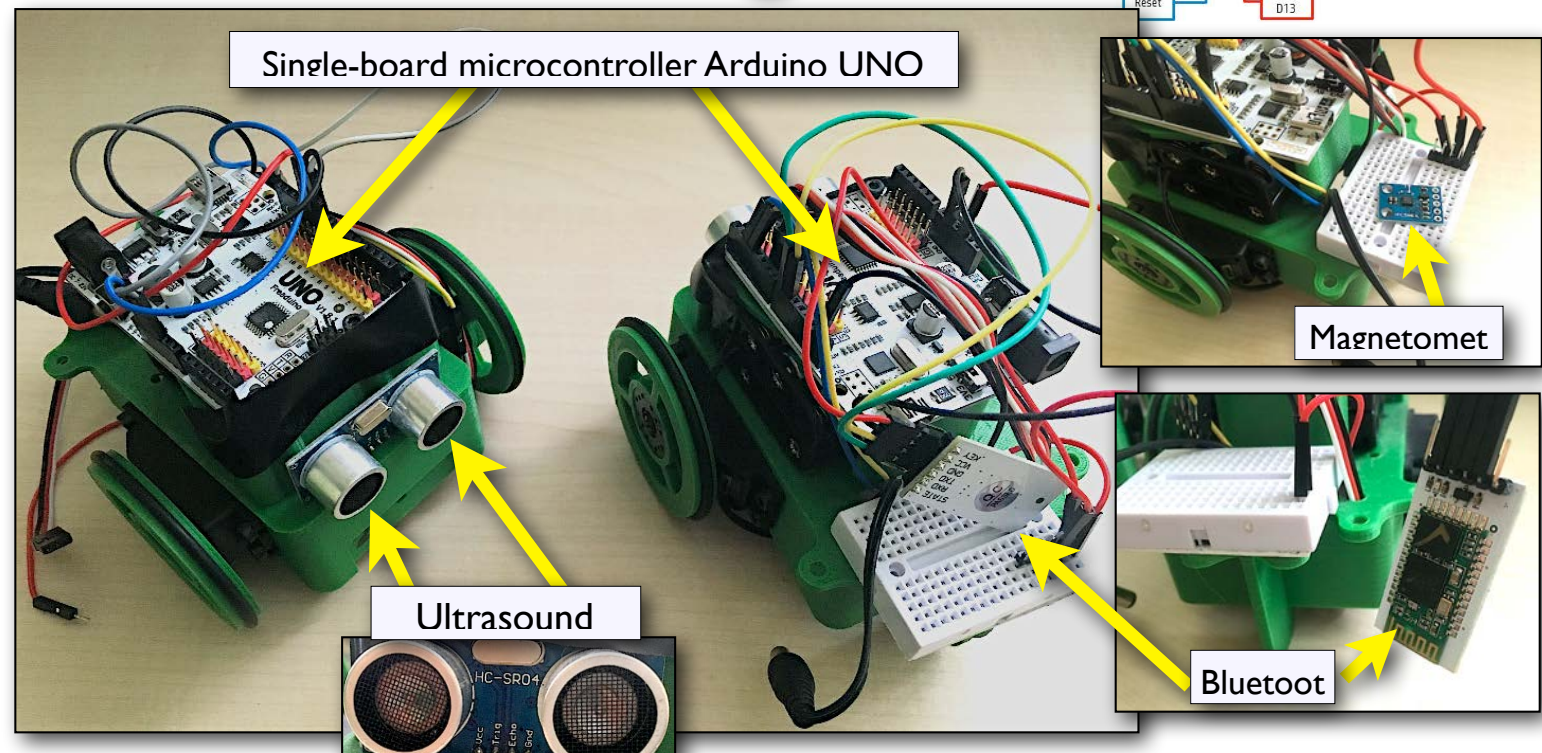
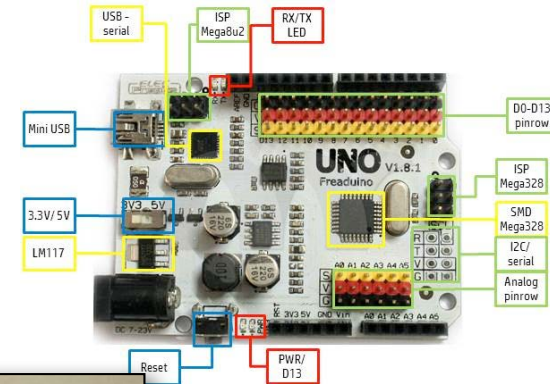
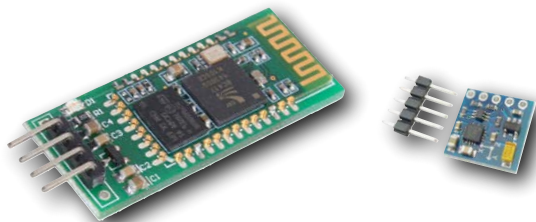
collision avoidance

magnetometers

global spatial orientation

bluetooth cards

wireless communication  
data exchange





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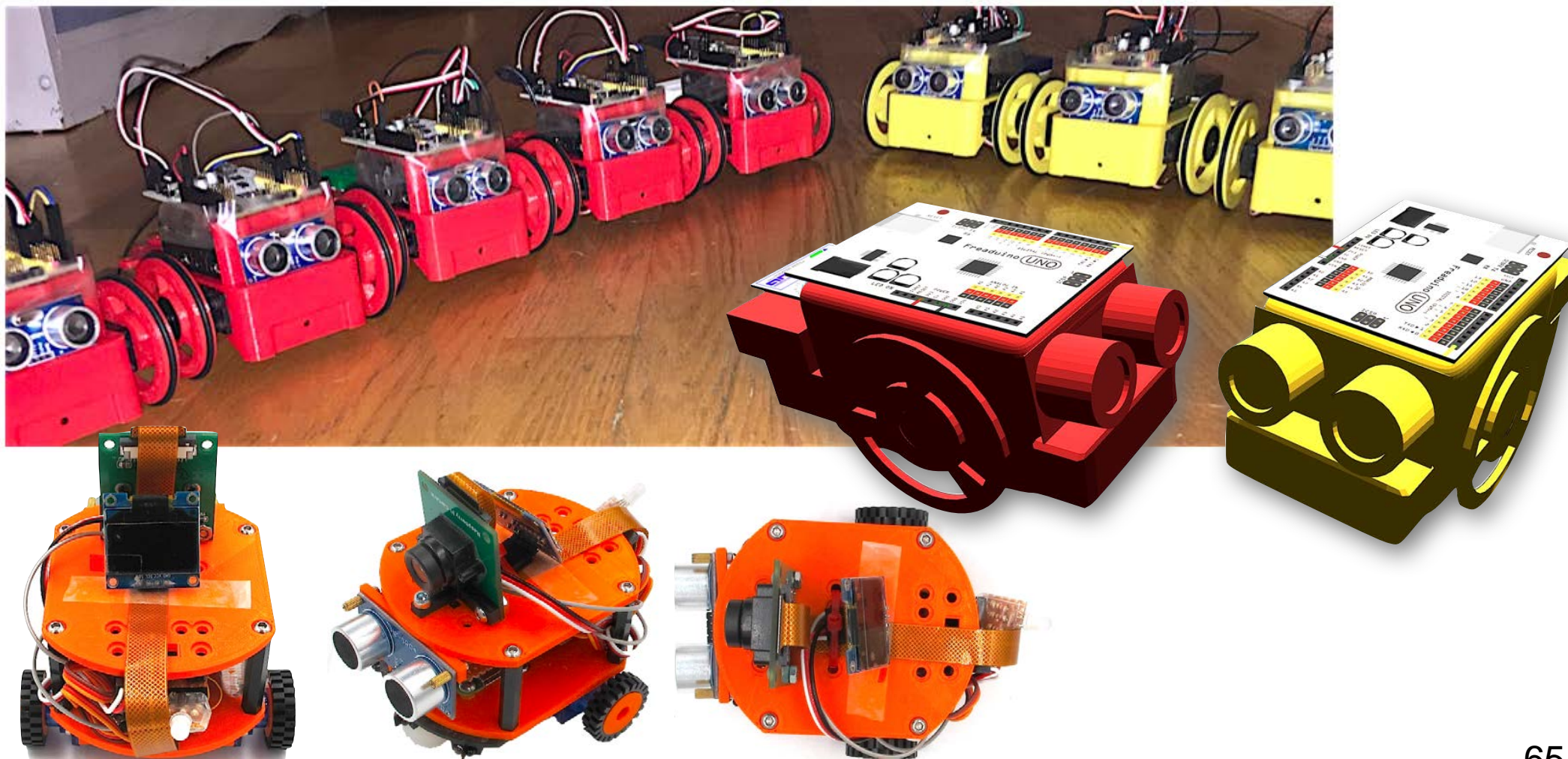
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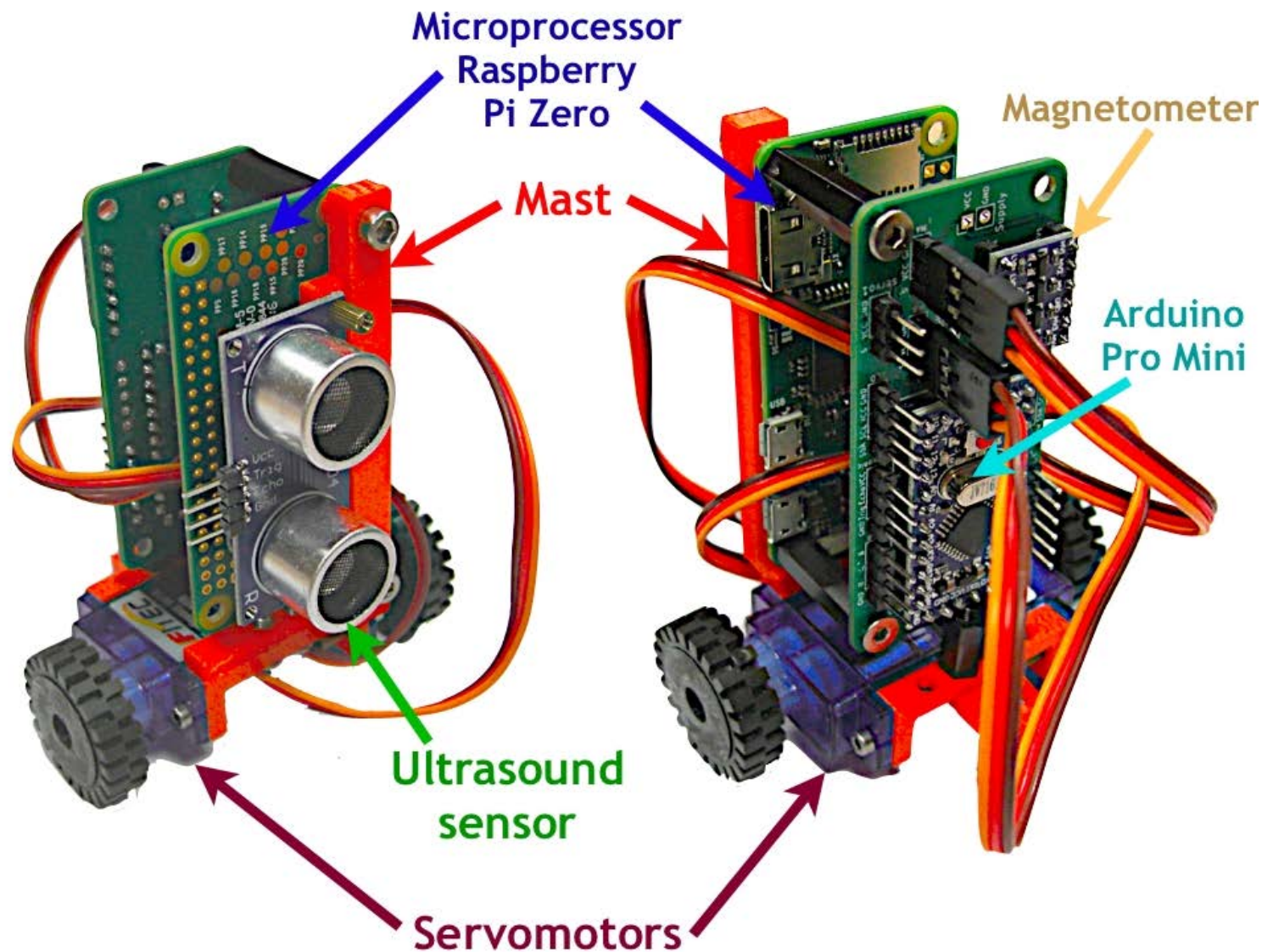
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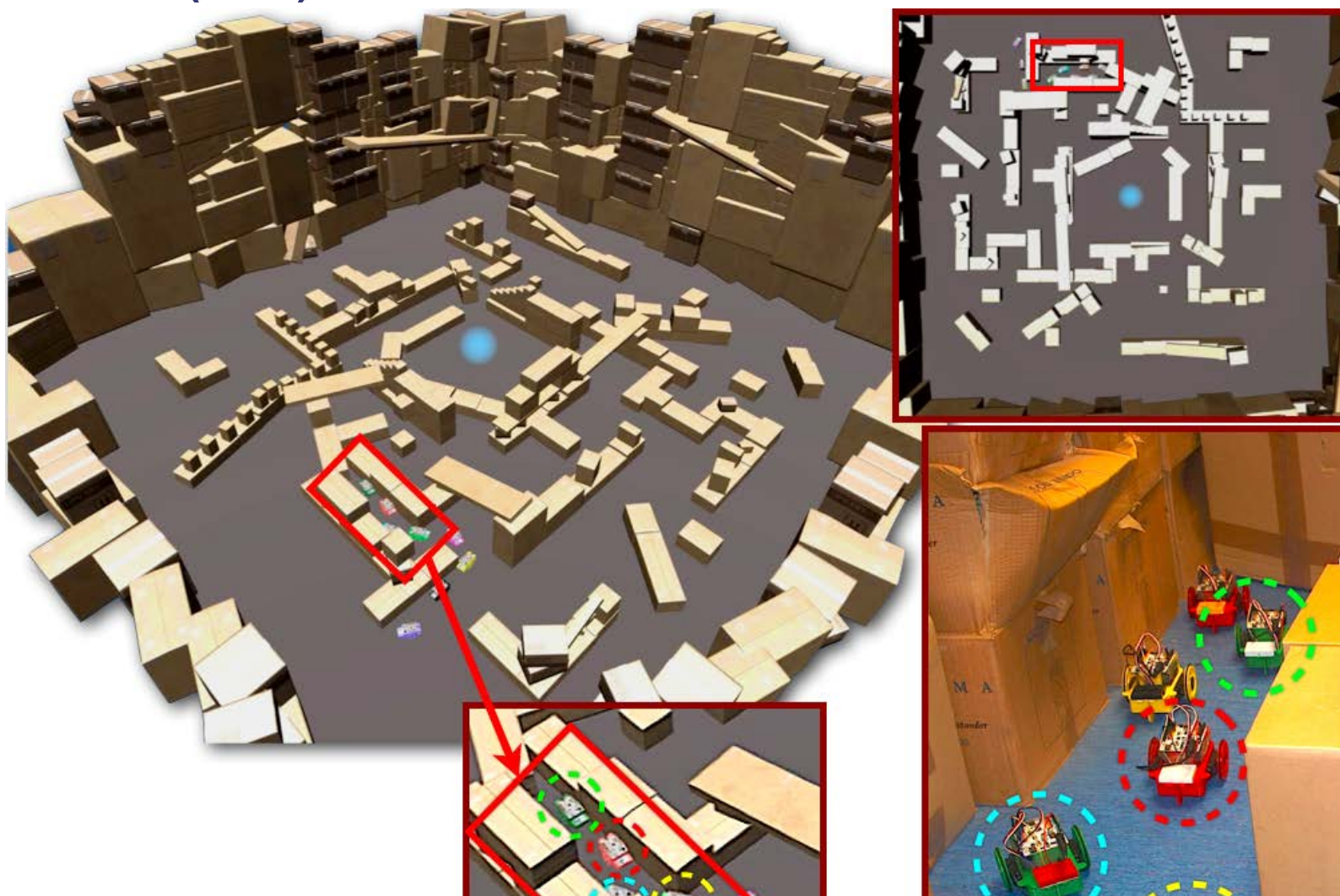


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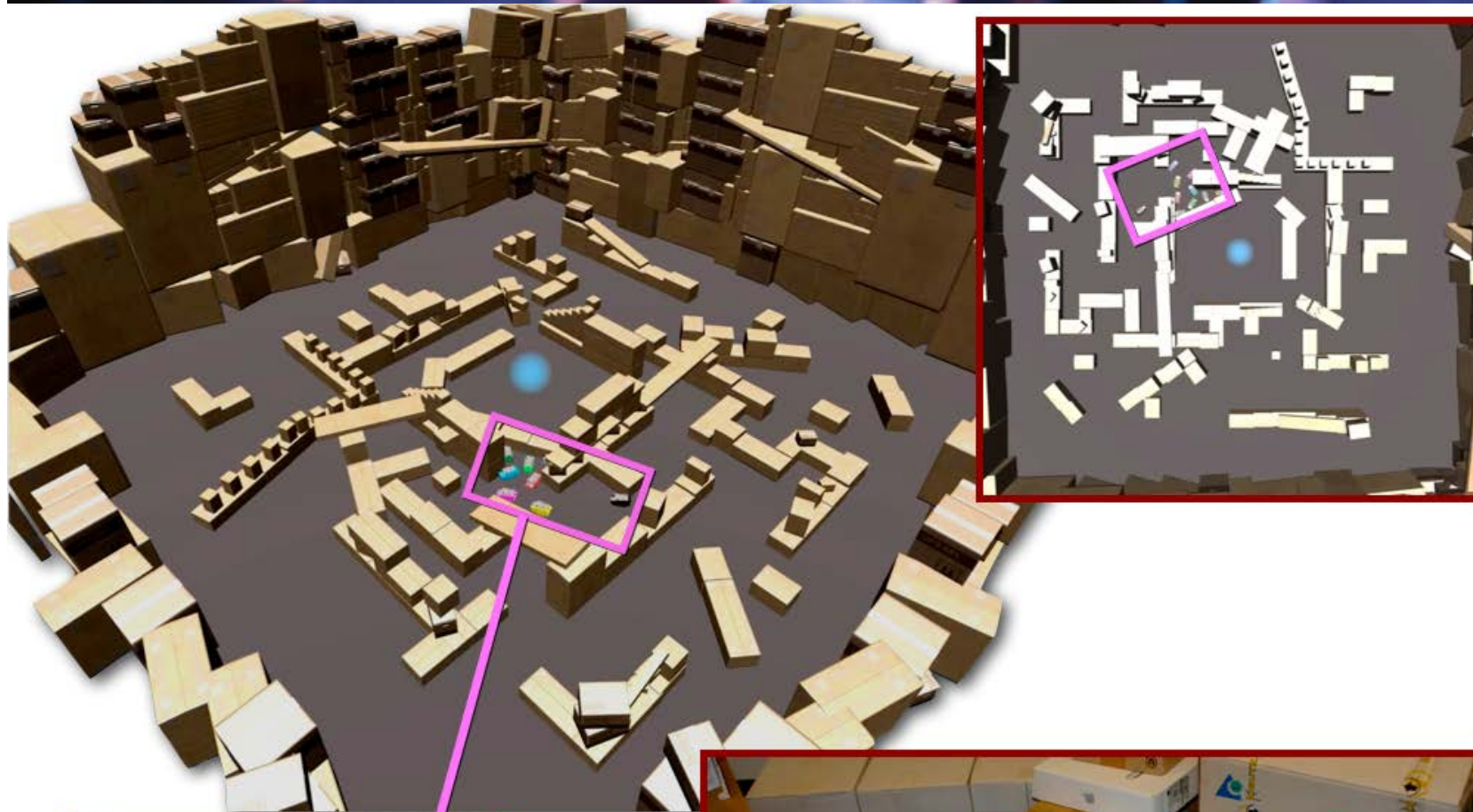
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**If you go to the website of this paper,  
you will find six videos available as  
supplementary material.**

Link: <https://www.sciencedirect.com/science/article/pii/S2210650217306338>



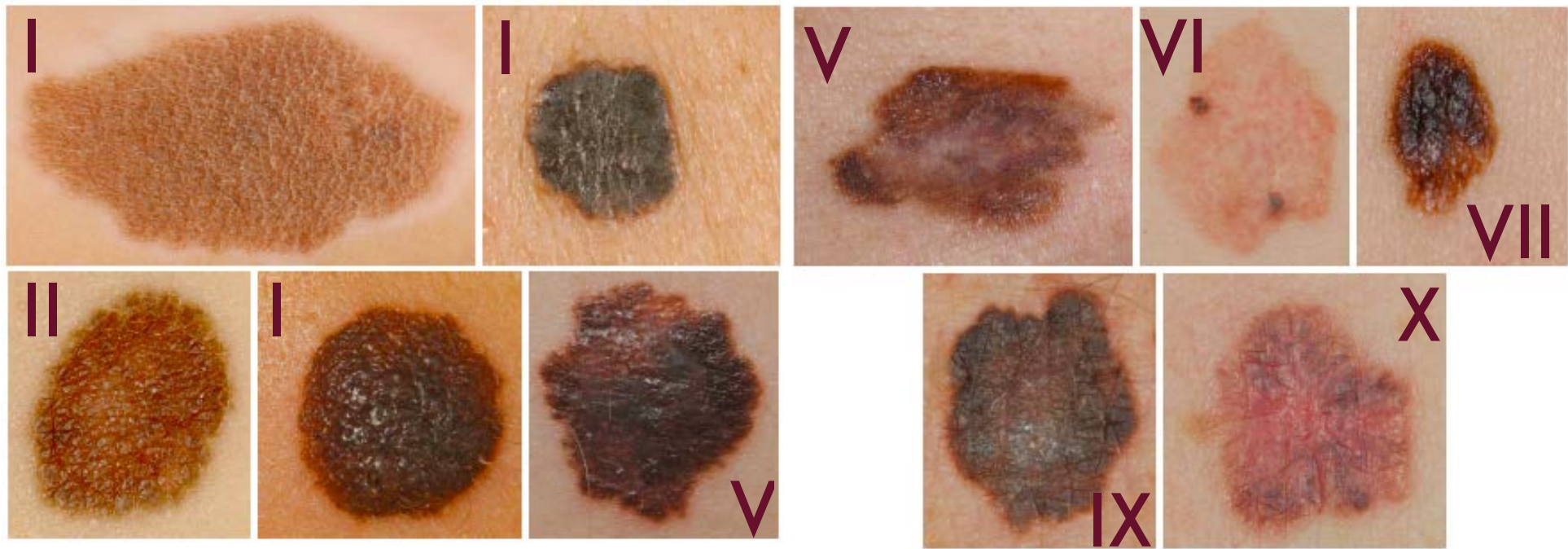
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**A Gálvez, A Iglesias: Memetic improved cuckoo search algorithm for automatic B-spline border approximation of cutaneous melanoma from macroscopic medical images. *Advanced Engineering Informatics*, (I.F. 8.8) Vol. 43, Paper 101005 (2020).**

**Malignant melanoma is the most frequent and most dangerous type of skin cancer (3.1 million cases with 60,000 deaths in 2015 worldwide)**

**Can you tell me which ones of the next images do correspond to benign and malignant skin lesions?**





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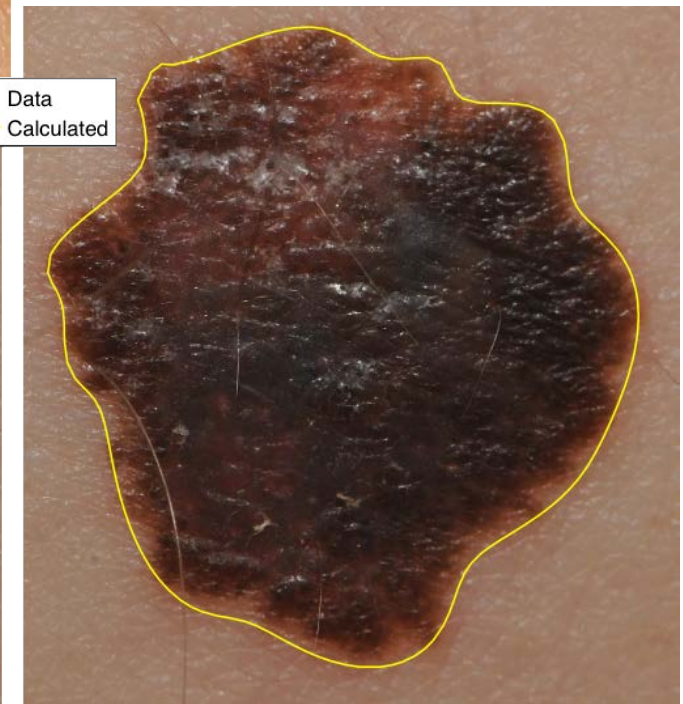


Example I

Example II

**A Gálvez, A Iglesias: Memetic improved cuckoo search algorithm for automatic B-spline border approximation of cutaneous melanoma from macroscopic medical images.**

**Advanced Engineering Informatics, (I.F. 8.8) Vol. 43, Paper 101005 (2020).**





## Conclusions

In this talk, I revised the potential role of AI and PDE for the problem of **shape reconstruction** from heterogeneous data sources (point clouds, multi-view images, cross-sections, vertex frames, mixed inputs).

This kind of complex & ambitious problems are more suitable for an international and multidisciplinary approach. This problem has been addressed in the European Union project PDE-GIR (2018-2023).

The developed methods have been applied to several challenging problems in computer design & manufacturing, computer graphics & animation, robotics, medical imaging, image processing, and others.

The **results are promising** and show the potential of this technology towards its application to several academic, business and industrial fields.



## Future Research

A critical limitation is that some problems still require some **manual intervention** at some steps of the process (i.e., sketch modeling medical imaging).

AI is the key to develop **automatic procedures** for model selections and other operations. The ability of AI systems to learn (from data, by examples) can help to fully automate the processes.

We aim at **extending the technology** developed in this project to other important applied problems in several fields.

Also, **international cooperation** is increasingly important in this area. We are open to potential collaborations with research and business stakeholders.



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End of the talk

## Thank you very much for your attention

### *Acknowledgements*

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